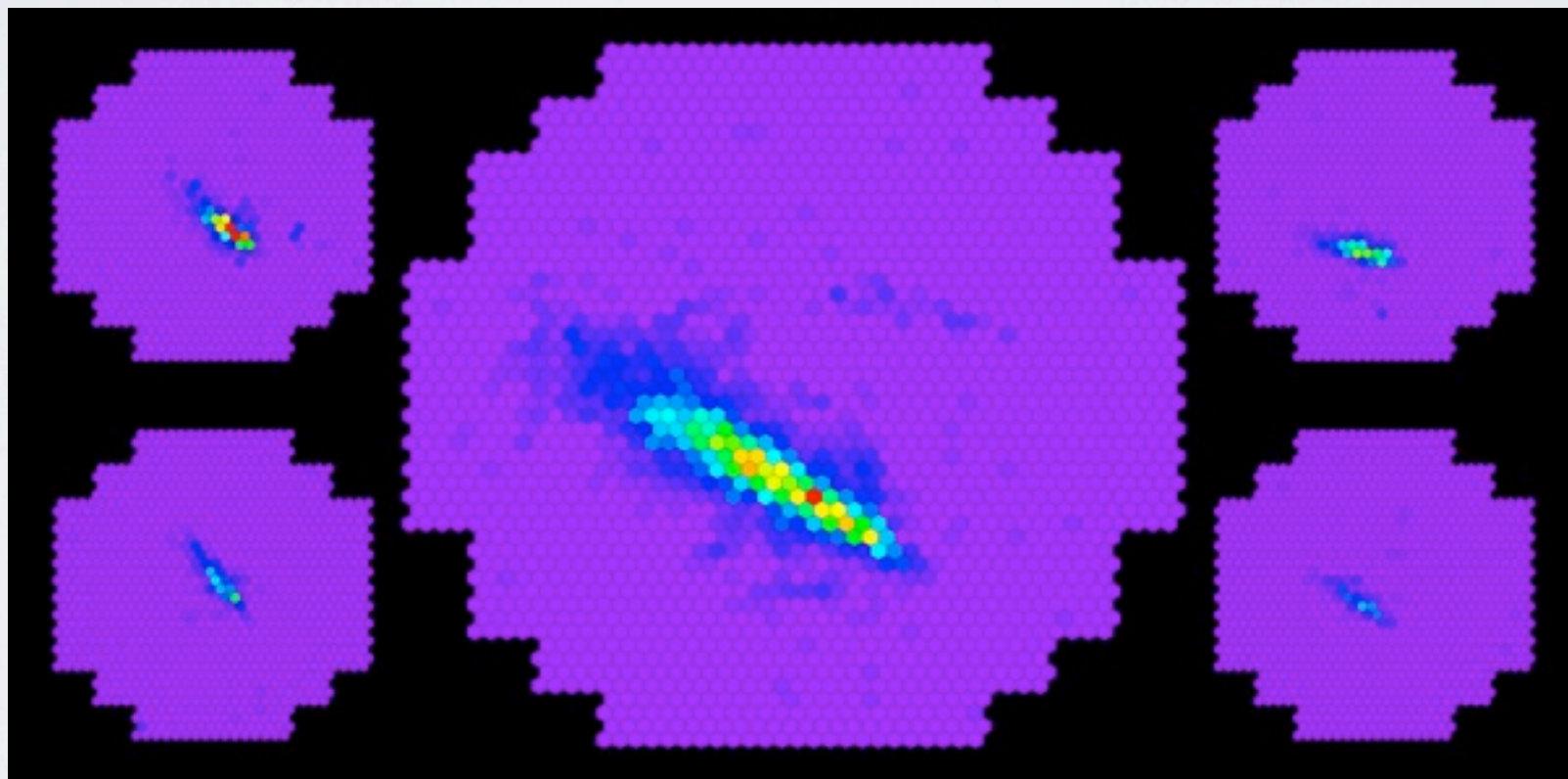


ON THE ANNIHILATION OF WIMPS

Matthew Baumgart (Carnegie Mellon U.)



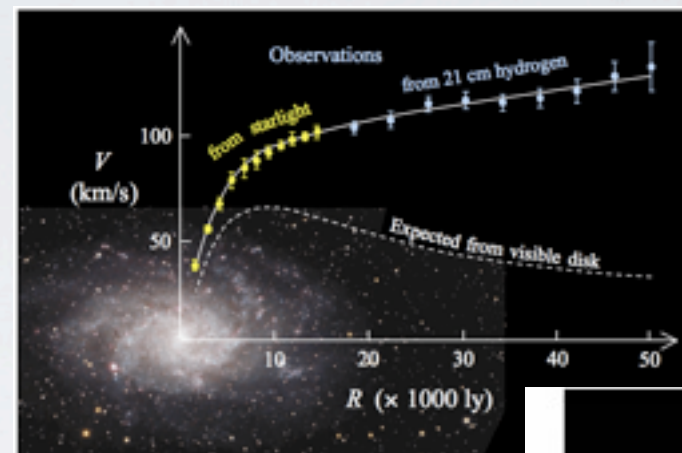
University of Massachusetts Amherst

1/30/2015

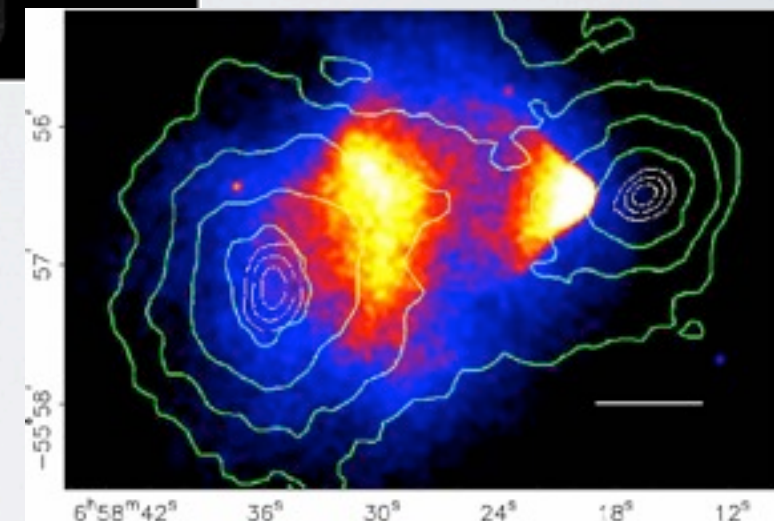
DARK MATTER

Dark Matter (DM) posited since 1930s (Zwicky, Oort, Rubin...) to explain variety of astrophysical anomalies

- Key questions about missing 27% of universe's energy
- **Does it interact with us nongravitationally?**
- **What are its quantum numbers?**
- Variety of motivated candidates (axions, asymmetric, sterile neutrinos...), but we focus on:
Weakly-Interacting Massive Particles (WIMPs)



DM at 3 scales:
Galaxy, Cluster, and
Cosmological



Parameter	Planck	
	Best fit	68% limits
$\Omega_b h^2$	0.022068	0.02207 ± 0.00033
$\Omega_c h^2$	0.12029	0.1196 ± 0.0031
$100\theta_{MC}$	1.04122	1.04132 ± 0.00068
τ	0.0925	0.097 ± 0.038
n_s	0.9624	0.9616 ± 0.0094
$\ln(10^{10} A_s)$	3.098	3.103 ± 0.072
Ω_Λ	0.6825	0.686 ± 0.020
Ω_m	0.3175	0.314 ± 0.020

WHY WIMPS?

- General consideration of particle DM in cosmology lead to “WIMP miracle”
- Particle freezes out when annihilation rate drops below cosmic expansion

$$n(T_f)\langle\sigma v\rangle \sim \left(H \sim \frac{T_f^2}{M_{Pl}} \right)$$

- Frozen out particle has density ratio to photons today as at freezeout

$$\frac{n_{X0}}{T_0^3} \simeq \frac{n(T_f)}{T_f^3}$$

- This lets us calculate relic density of dark matter...

$$\Omega_X h^2 \equiv \frac{\rho_{X0}}{\rho_c} h^2 \sim \frac{M_X}{T_f} \frac{1}{3 \times 10^4} \frac{1}{\langle\sigma v\rangle} \frac{1}{T_0 M_{Pl}} \sim \frac{1}{10^3 \langle\sigma v\rangle} \frac{1}{\text{TeV}^2}$$

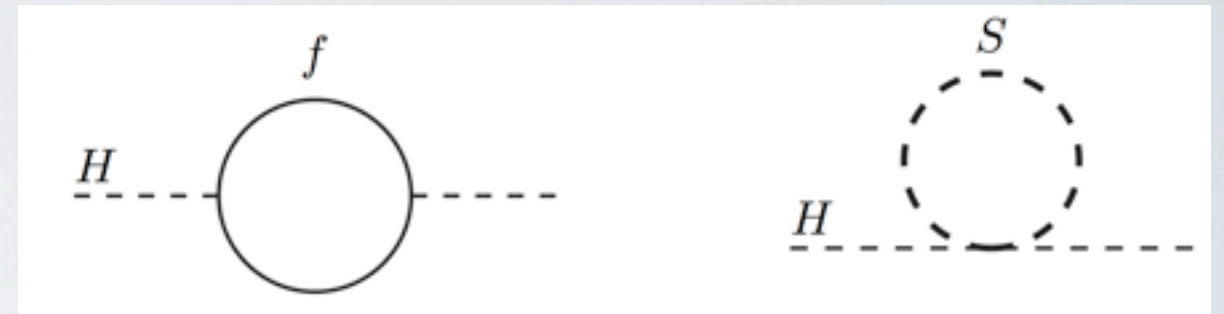
- ...and expected mass given a perturbative annihilation process $\langle\sigma v\rangle \sim C \alpha^2/M_X^2$

$$M_X \sim \text{TeV} \left(10\sqrt{C}\alpha \right) \sqrt{\frac{\Omega_X h^2}{0.12}}$$

SUPERSYMMETRY

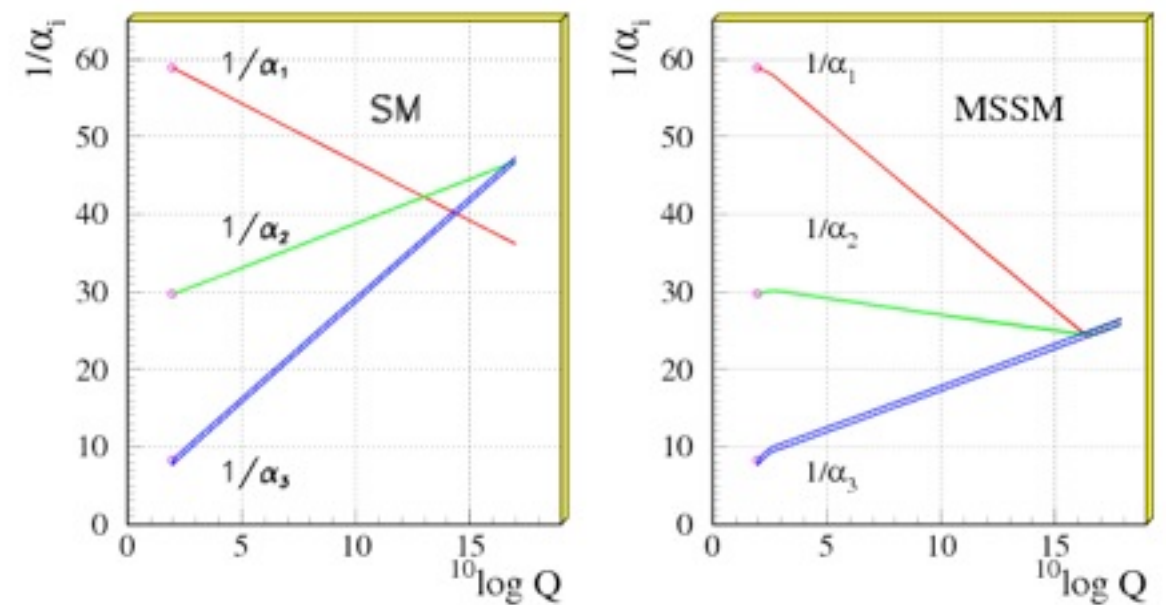
- Supersymmetry: Unique extension of global spacetime symmetries of special relativity*
- Posits **bosonic partner for all fermions** with same quantum numbers (and **vice versa**)
- Discrete symmetry to **protect proton** (R-parity) provides a **new stable particle** (LSP)
- Connecting **SUSY** to weak scale thus gives **natural WIMP** dark matter

*Haag et al. NPB 88(1975): 257-74



SUSY ties superpartner masses and weak scale in most of its parameter space

Unification of the Coupling Constants in the SM and the minimal MSSM



Strongest indirect evidence for weak-scale SUSY possibly the **unification of gauge couplings**

FROM WIMP TO WINO

- Without any input of electroweak physics, cosmology gives us Weak-scale (TeV) with weak couplings
- Tempting to connect Dark Matter to Hierarchy Problem as in SUSY
- What are motivated candidates and how do we find/exclude them?

Supersymmetry (SUSY):
Natural DM candidates,
Grand Unification
Hierarchy Problem
Quantum Gravity
Mini-split → Anomaly Mediation

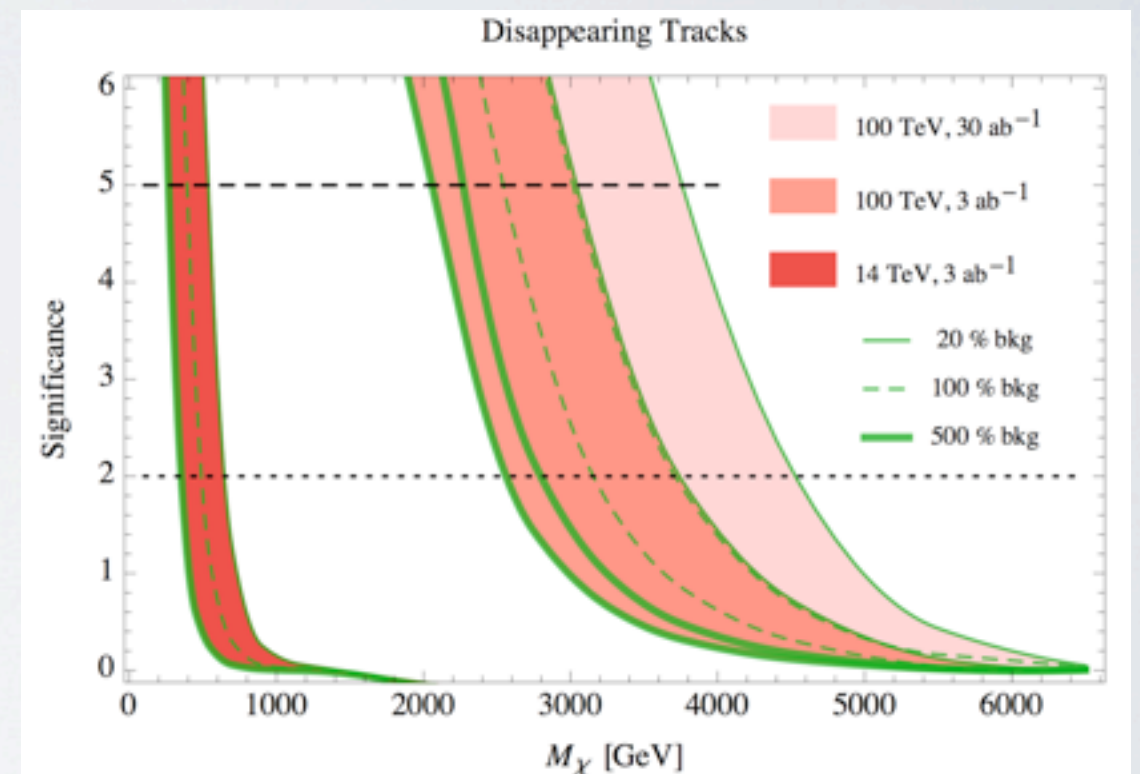
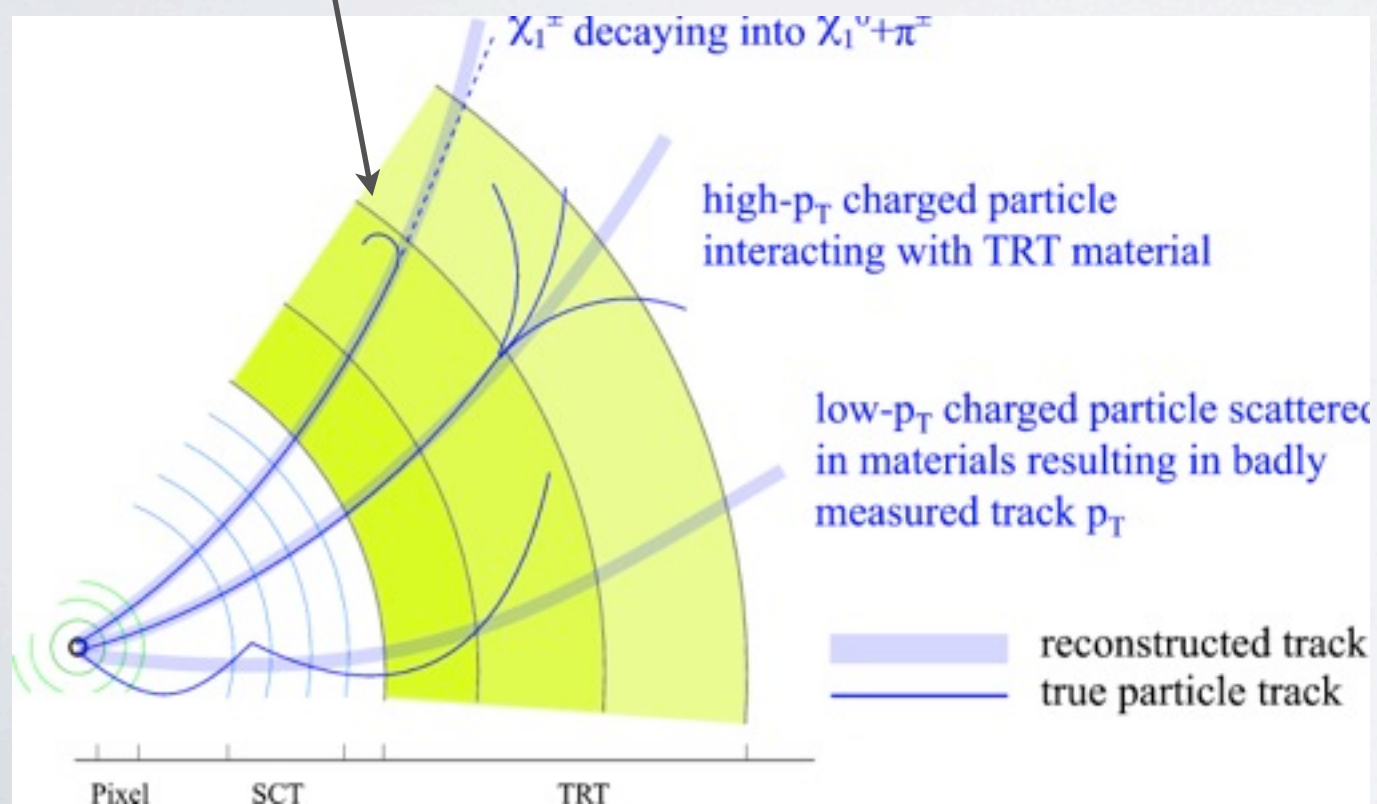
Bottom-up:
What's a simple
Standard Model
Extension that could be
Dark Matter?

SU(2)-triplet fermion
“wino”

TO FIND A TEV WINO

- **LHC:** Small mass splitting between χ^\pm and χ^0 ($\Delta M = 165$ MeV) makes disappearing track $O(10\text{cm})$

Current limit $M_\chi > 270$ GeV

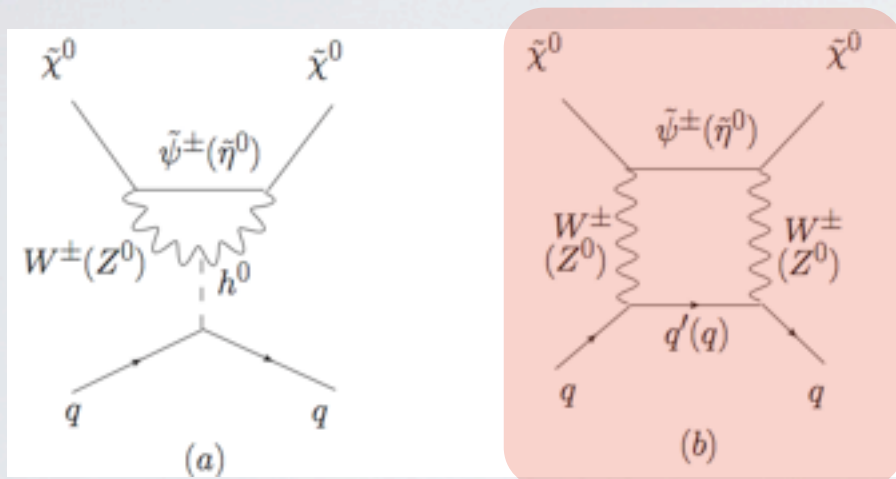


From Cirelli et al. 1407.7058

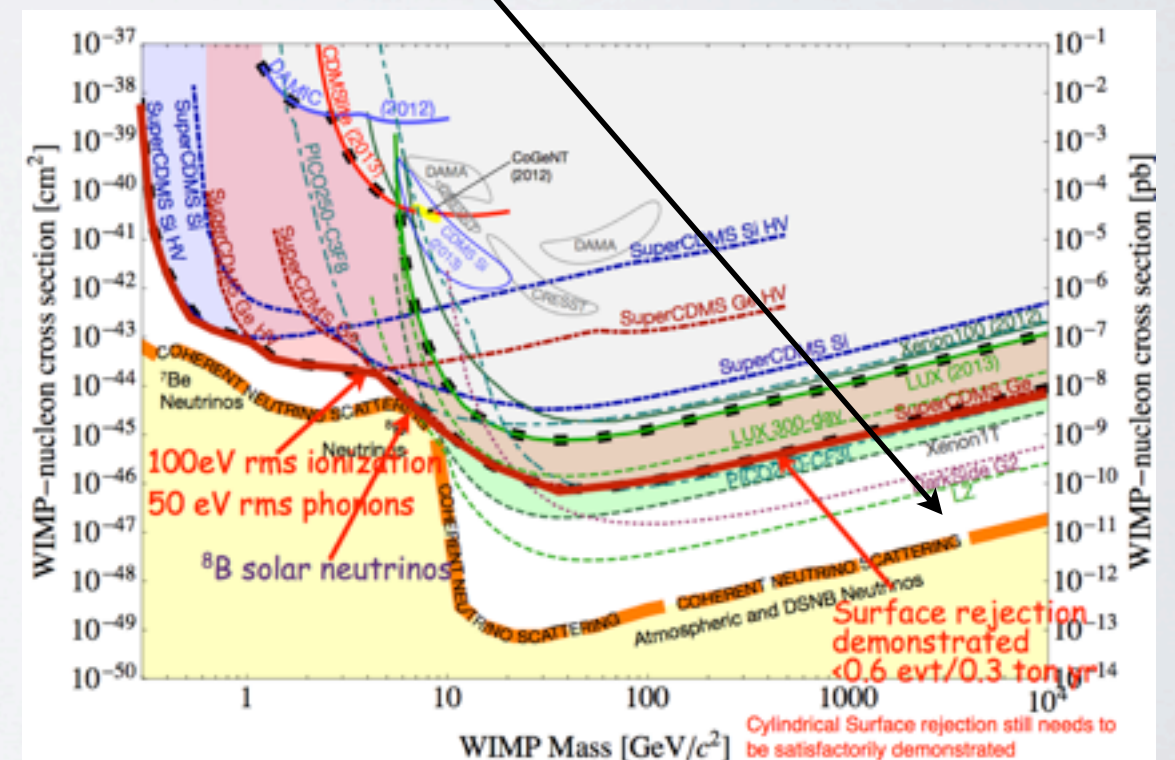
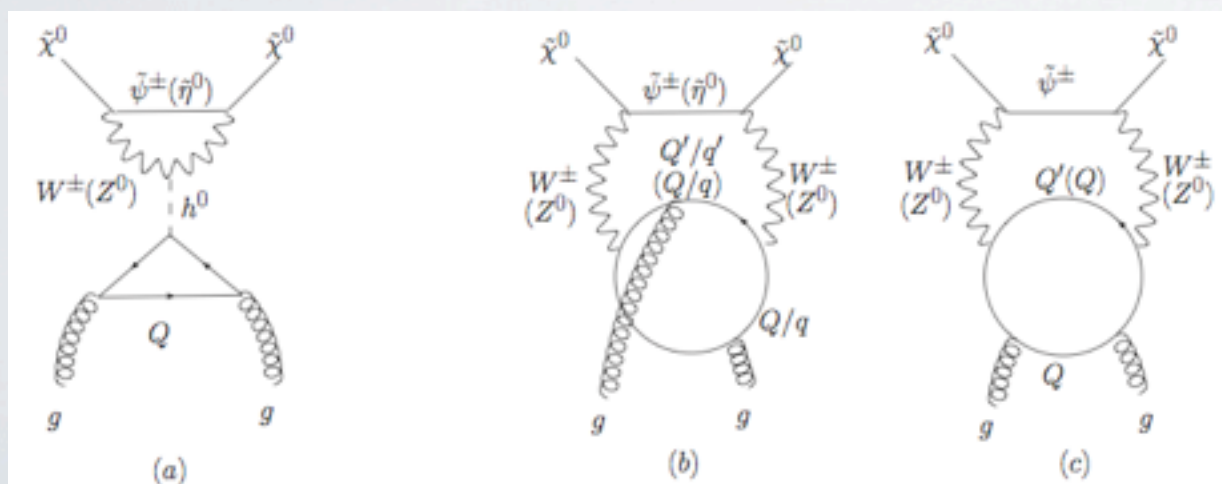
1202.4847 (ATLAS)

TO FIND A TEV WINO

Direct Detection: Wino has no renormalizable couplings to Z-boson or Higgs
Cross section proceeds through loops, which partially cancel for $m_h = 125$ GeV

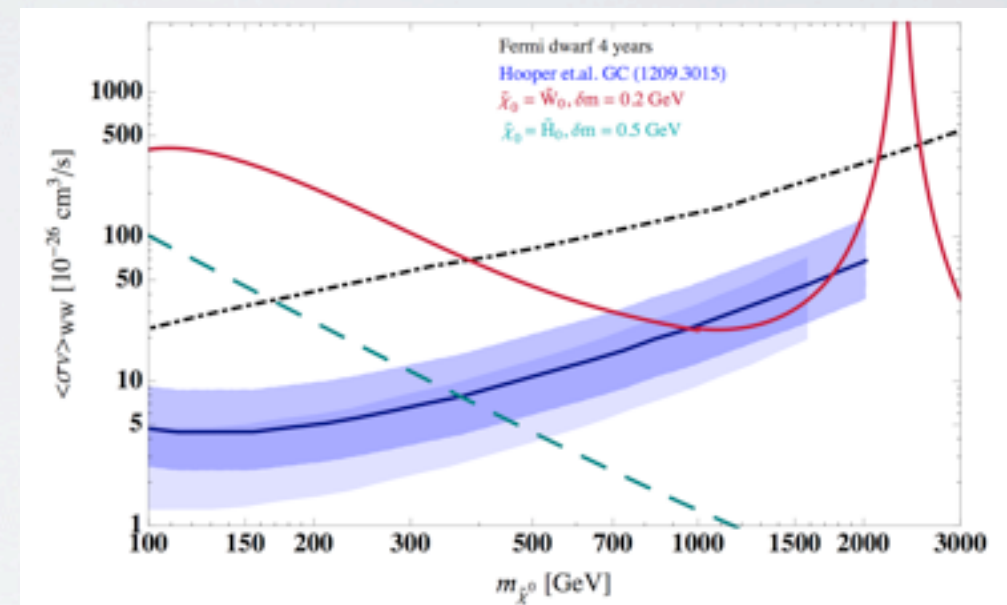
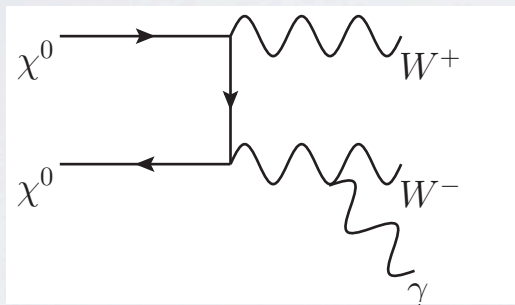


Highlighted diagram gives negative contribution, all others positive, $\sigma \sim 10^{-47} \text{ cm}^2$



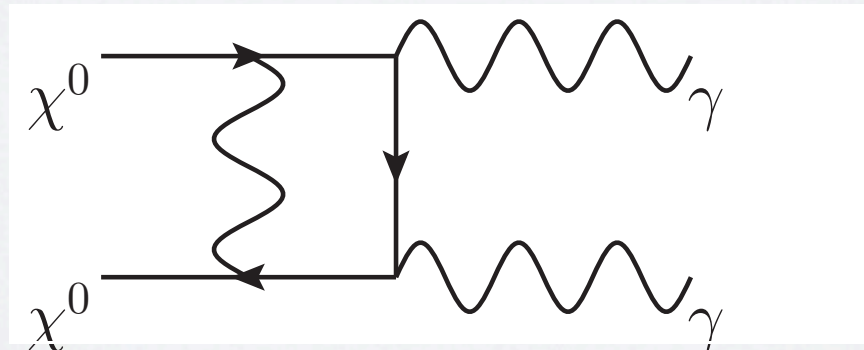
INDIRECT DETECTION

- **Continuum** ($\chi\chi \rightarrow W^+W^- \rightarrow \text{photons}$) useful for **sub-TeV** limits (Fermi)



- **Line** ($\chi\chi \rightarrow \gamma + X$) extends to multi-TeV range

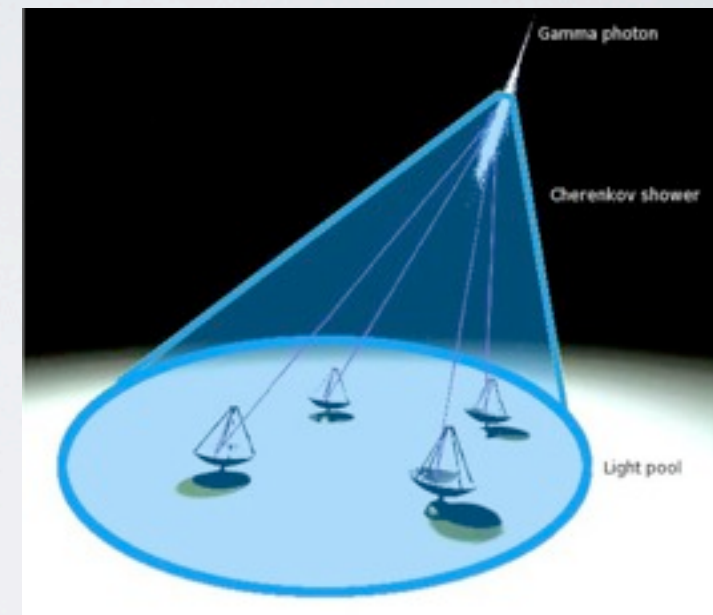
J. Fan & M. Reece: 1307.4400



HESS



- High Energy Stereoscopic System (HESS)
- Atmospheric Cherenkov telescope
- Constrains photon lines. Our main interest...



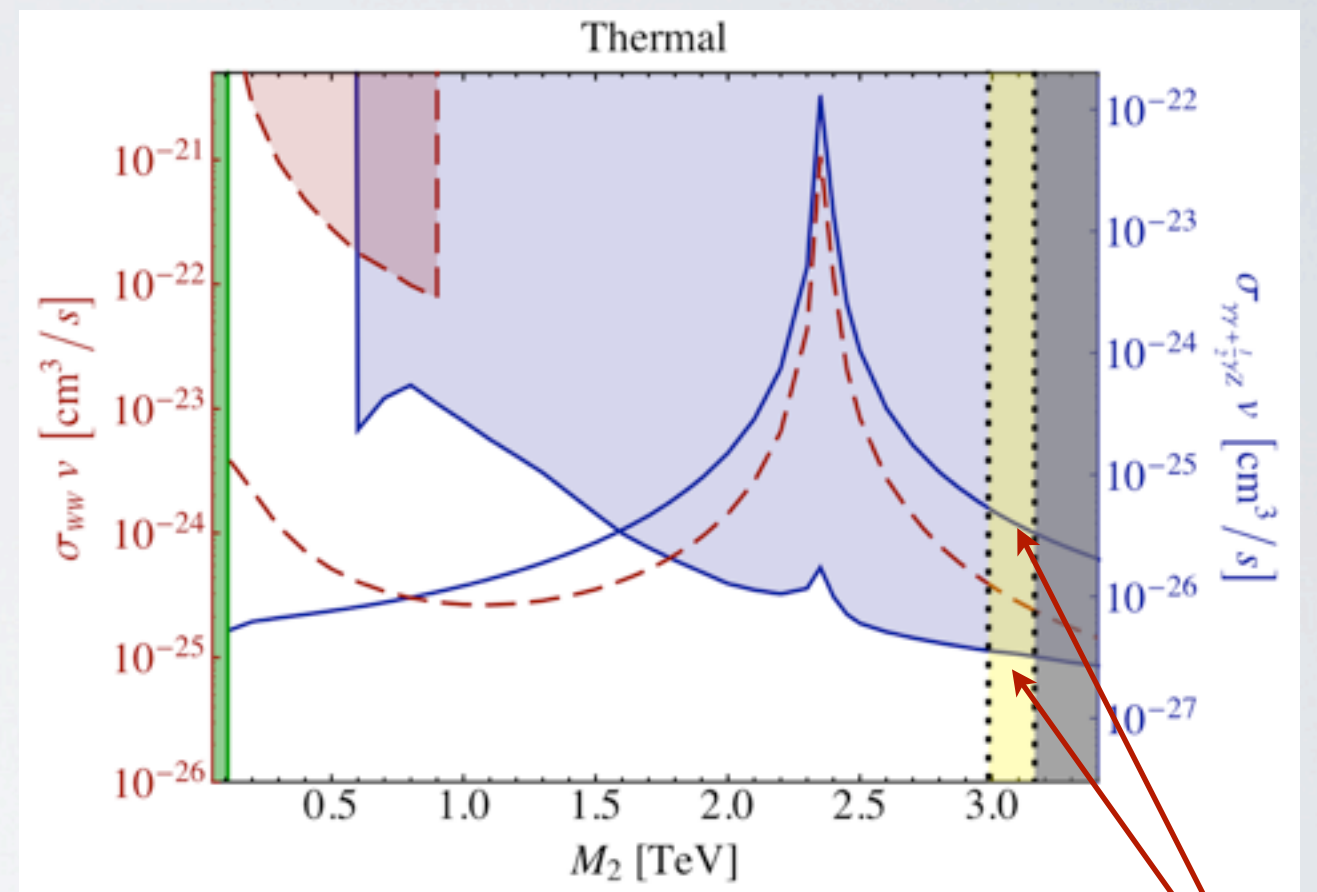
$O(\text{TeV}) \gamma$
leads to
 $O(10^4\text{m})$
light pool
on ground

Schematic of air shower observed by Cherenkov Telescope (spie.org)



“WINO DARK MATTER UNDER SIEGE”*

- Annihilation of neutral wino, $\tilde{\chi}$, through gauge interactions to SM states (e.g. $\tilde{\chi}\tilde{\chi} \rightarrow \gamma\gamma$) gives $M \approx 3 \text{ TeV}$
- Has our beautiful, simple model been **shot dead by HESS?**
- Navarro-Frank-White (cusped) halo profile assumed



From I 307.4082:
 Blue line: Wino annihilation rate
 Blue shade: Exclusion from HESS
 Yellow shade: All DM is thermal wino

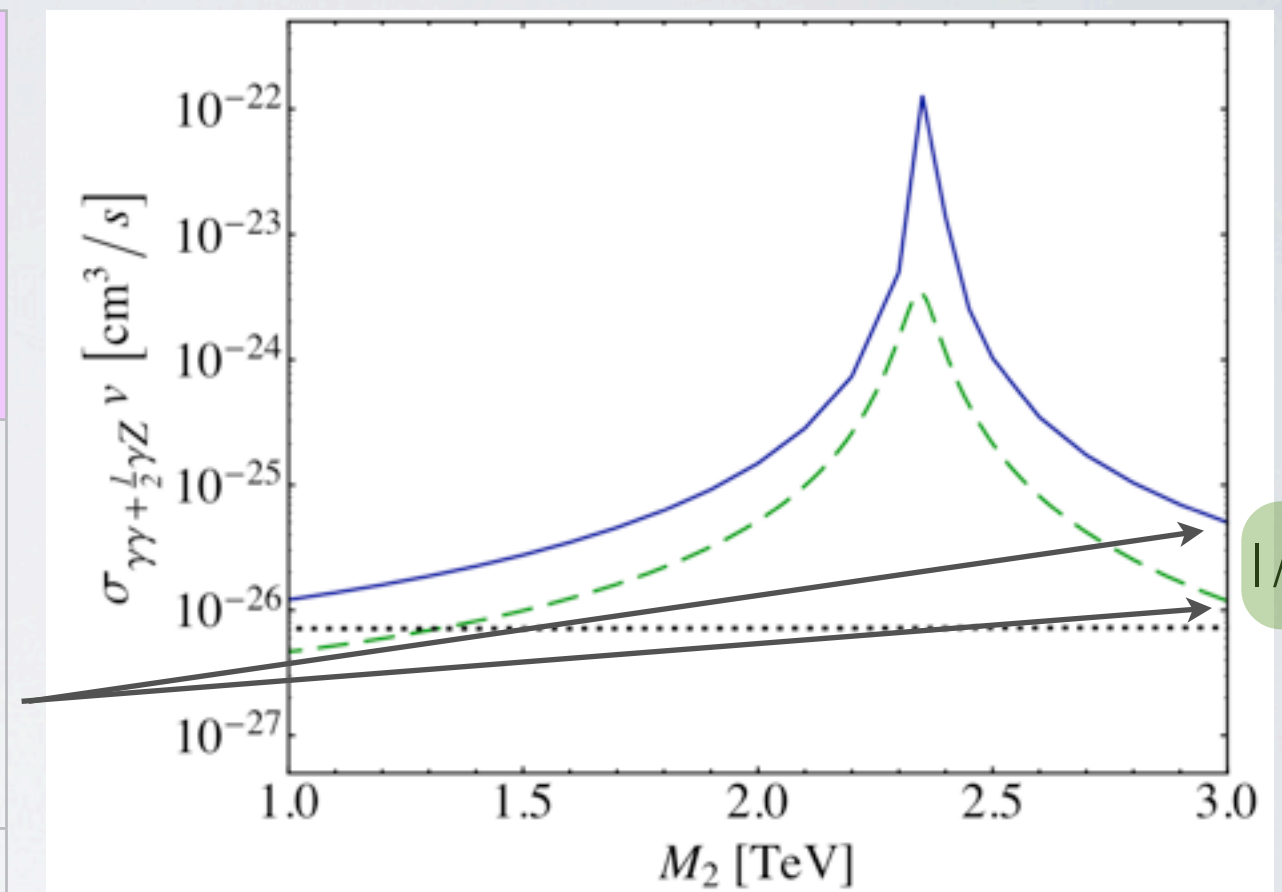
Ruled out by I 6x?

* I 307.4082: Cohen, Lisanti, Pierce, and Slatyer; see also “In Wino Veritas”, I 307.4400: Fan & Reece

WHAT COULD SAVE THE WINO?

Halo Model	Radiative Corrections
Flatten distribution in galactic center (core)	Claim in literature of 75% reduction at NLO
Core needed: 1.5 kpc	Core needed: 0.5 kpc

Simulations with baryons show **cusped profiles down to 1 kpc** (1208.4844, 1305.5360, 1306.0898)



From Cohen et al. 1307.4082

Factor of few at stake,
need state of the art calculation
to determine

WINOS BEYOND PERTURBATION THEORY*

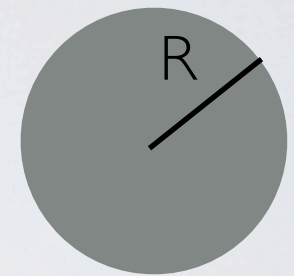
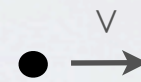
- There are reasons to think wino annihilation in the present-day may receive large higher-order corrections:
- Slowly-moving ($v \sim 10^{-3}$) winos' annihilation rate subject to **Sommerfeld Enhancement**. Higher perturbative order brings in new channel.
- **Sudakov double-logarithms**: Large in electroweak physics, even in inclusive observables. **Can't trust fixed order.** We must resum logs.

*MB, Rothstein, I and Vaidya, V:
1409.4415 & 1412.8698

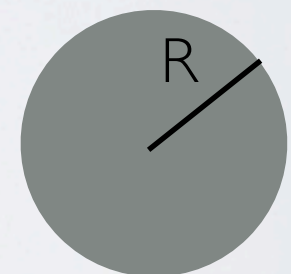
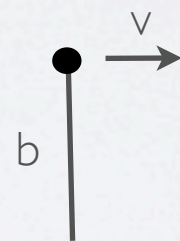
SOMMERFELD ENHANCEMENT

- Slowly-moving objects in a potential can have **much larger cross section** than perturbative treatment suggests
- Quantum-Mechanically, short-distance annihilation rate modified by **wavefunction-at-origin** in presence of potential:

$$\langle \sigma v \rangle = |\psi(0)|^2 \Gamma_{\text{pert.}}$$



In absence of gravitation, capture radius is geometric, R



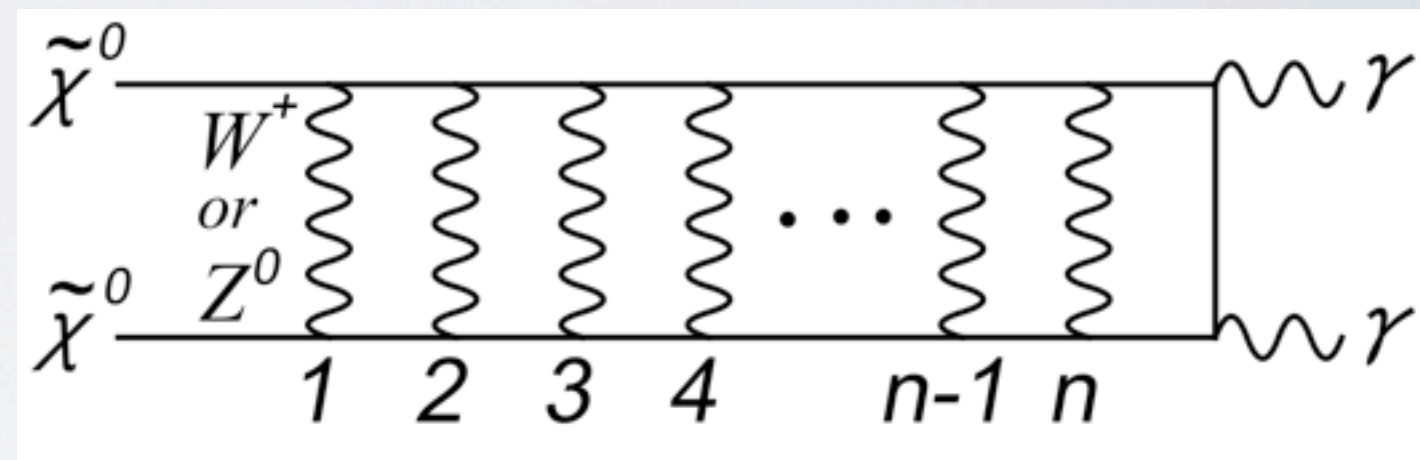
Turning on gravity, cross section grows for slower projectile:

$$b_{\text{capture}} = R \sqrt{1 + \frac{2GM}{v^2 R}}$$

SOMMERFELD & FIELD THEORY

Crossing lines
leads to $O(v)$
suppression
compared to
ladder

- In nonrelativistic regime, **summing infinite ladder exchange** equivalent to **solving Schrodinger equation** for appropriate potential
- W-exchanges flip between $\chi^0\chi^0$ and $\chi^+\chi^-$ states
- Ladder exchanges **unsuppressed**



From Hisano et al. hep-ph/0412403,
see also Arkani-Hamed et al.: 0810.0713,
Slatyer: 0910.5713

$$\mathcal{A}_n \simeq \alpha \left(\frac{\alpha_2 M}{m_W} \right)^n$$

ELECTROWEAK POTENTIAL*

- Potential accounts for Yukawa exchange of Ws, Zs, Coulomb exchange of γ s, and $\chi^+ - \chi^0$ mass splitting = (0.17 GeV)

$$\begin{pmatrix} 2\delta M - \frac{\alpha}{r} - \alpha_W c_W^2 \frac{e^{-m_Z r}}{r} & -\sqrt{2}\alpha_W \frac{e^{-m_W r}}{r} \\ -\sqrt{2}\alpha_W \frac{e^{-m_W r}}{r} & 0 \end{pmatrix}$$

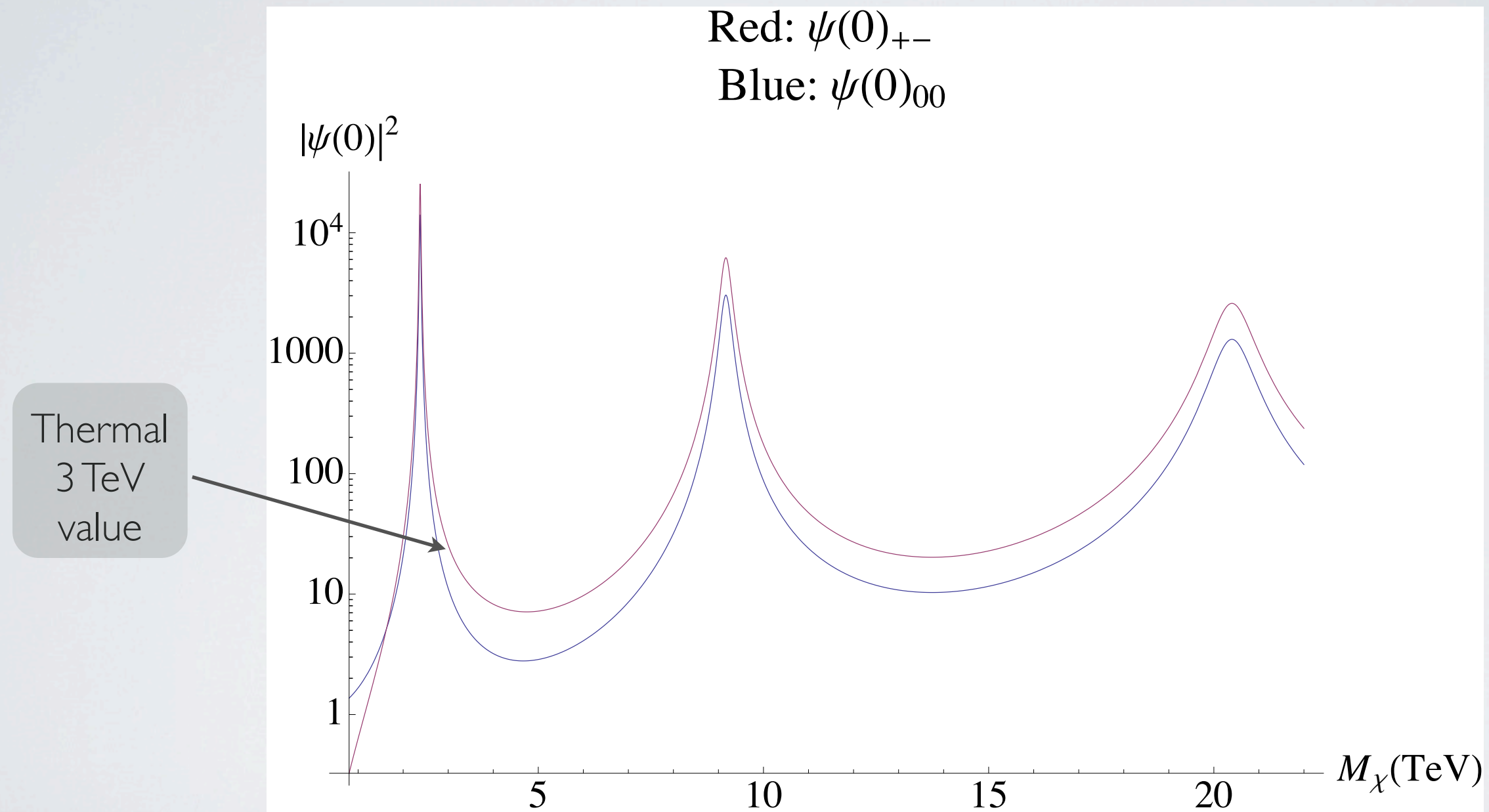
Mass splitting means +- state decays exponentially

- Between the two-body 1S_0 states with interpolating fields:

$$\frac{1}{\sqrt{2}}\chi^+(\vec{x} - \vec{r}/2)\chi^-(\vec{x} - \vec{r}/2) \quad \frac{1}{2}\chi^0(\vec{x} - \vec{r}/2)\chi^0(\vec{x} - \vec{r}/2)$$

*See also Hisano et al.: hep-ph/0412403

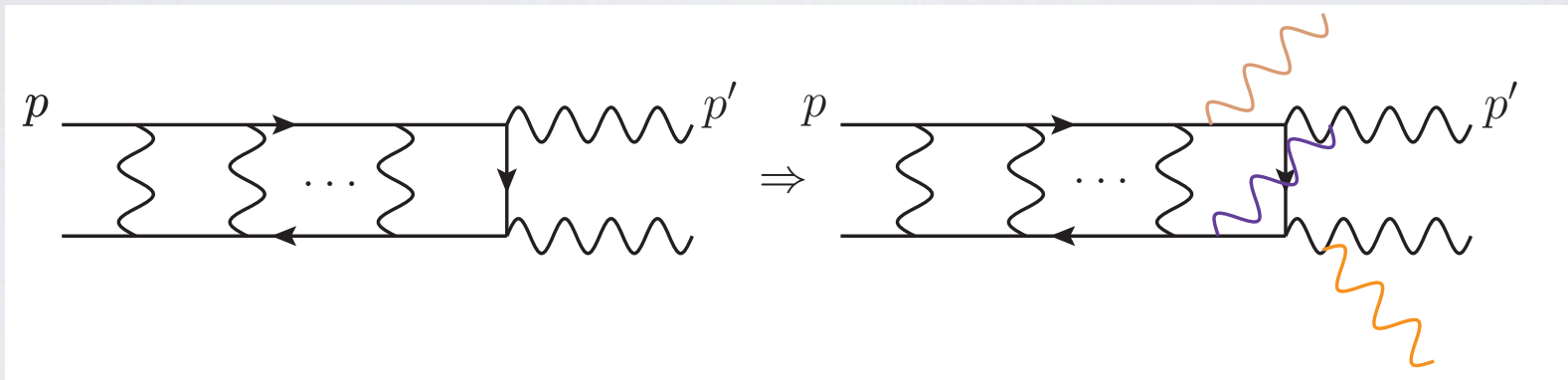
WINO SOMMERFELD FACTORS



Solving Schrodinger equation for $v = 10^{-3}$ gives us resonance regions with $O(10^4)$ enhancement

SUDAKOV LOGARITHMS

- Emission of **soft or collinear radiation** can lead to **infrared divergences**



- Accounting for extra emission enters multiplicatively as **Sudakov double logarithm**

$$d\sigma(p \rightarrow p' + \gamma) = d\sigma(p \rightarrow p') \frac{\alpha}{\pi} \log(Q^2/\mu^2) \log(Q^2/m^2)$$

- For wino annihilation at the thermal mass (3 TeV), another **challenge for perturbation theory** $\frac{\alpha_W}{\pi} \log(M_{\text{wino}}^2/m_W^2)^2 \approx 0.6$

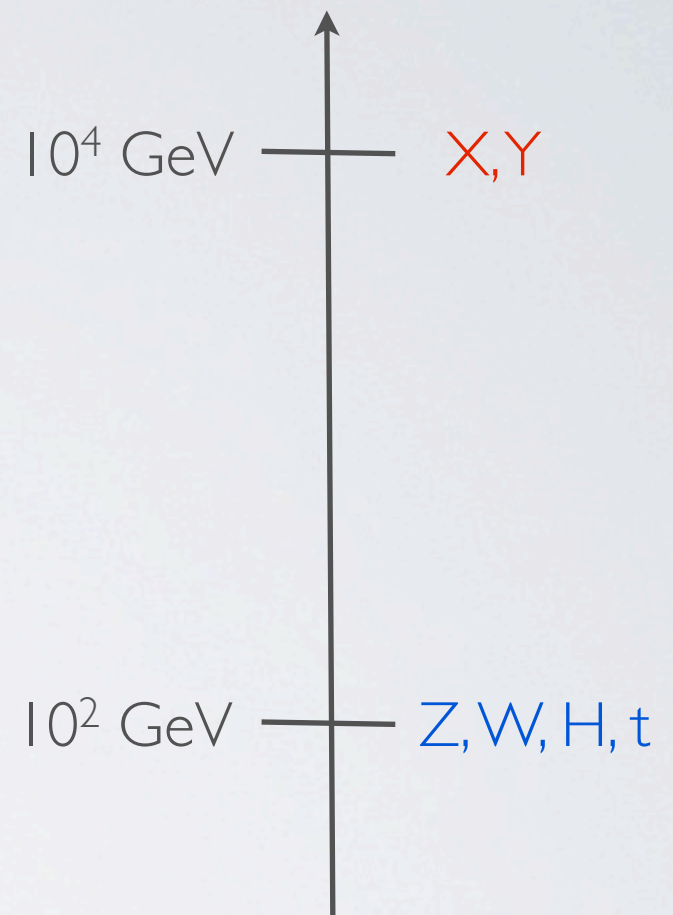
EFFECTIVE FIELD THEORY

- **Stuck** with large log, **we must resum** $\alpha \log^2$ to $\text{Exp}[C \alpha \log^2]$
- **Essential tool** of the modern, phenomenological field theorist
- **Systematically decouple** high-energy degrees of freedom to answer low-energy questions as in Wilsonian-RG

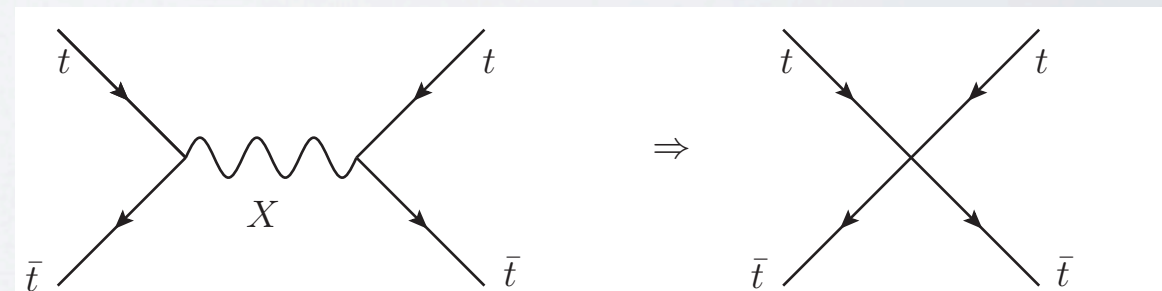
$$Z[\phi]_{\Lambda-\Delta\Lambda} = \int_{k \in (\Lambda-\Delta\Lambda, \Lambda)} \mathcal{D}\phi \exp[iS(\phi)]$$

- **Match** amplitudes as expansion in $1/M_X^2$, α

Resum logs $\log(M_X/m_t)$ by running in EFT



Schematic for simple EFT, where **X,Y integrated out** to generate **new interactions for SM fields**



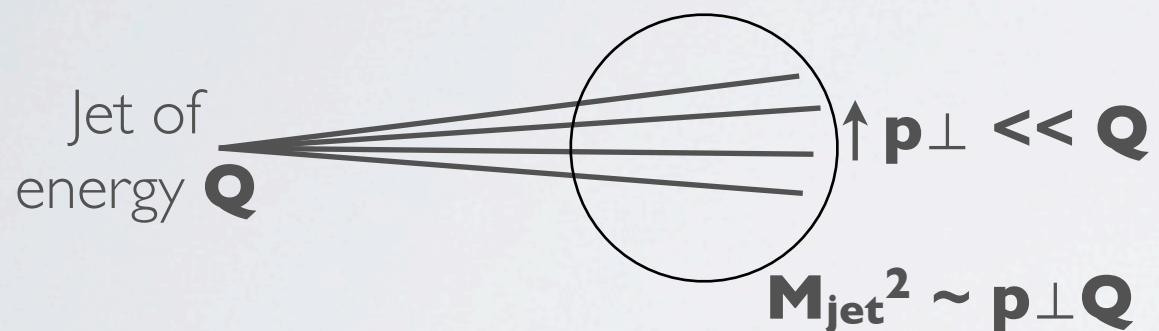
SOFT-COLLINEAR EFFECTIVE THEORY

Lightcone momenta

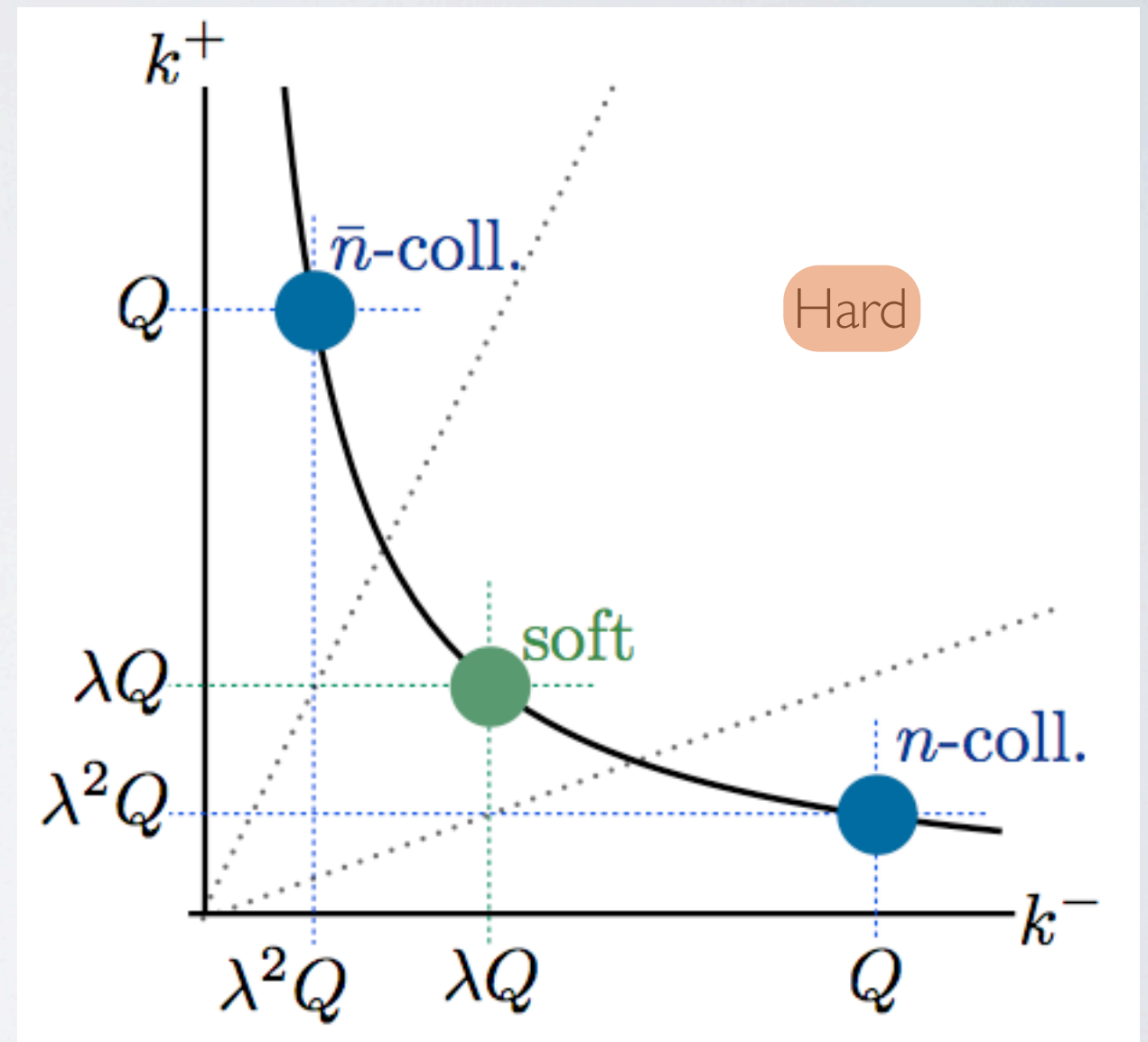
$$k^+ = k^0 + k^3$$

$$k^- = k^0 - k^3$$

- Large scale-hierarchies can arise within one field



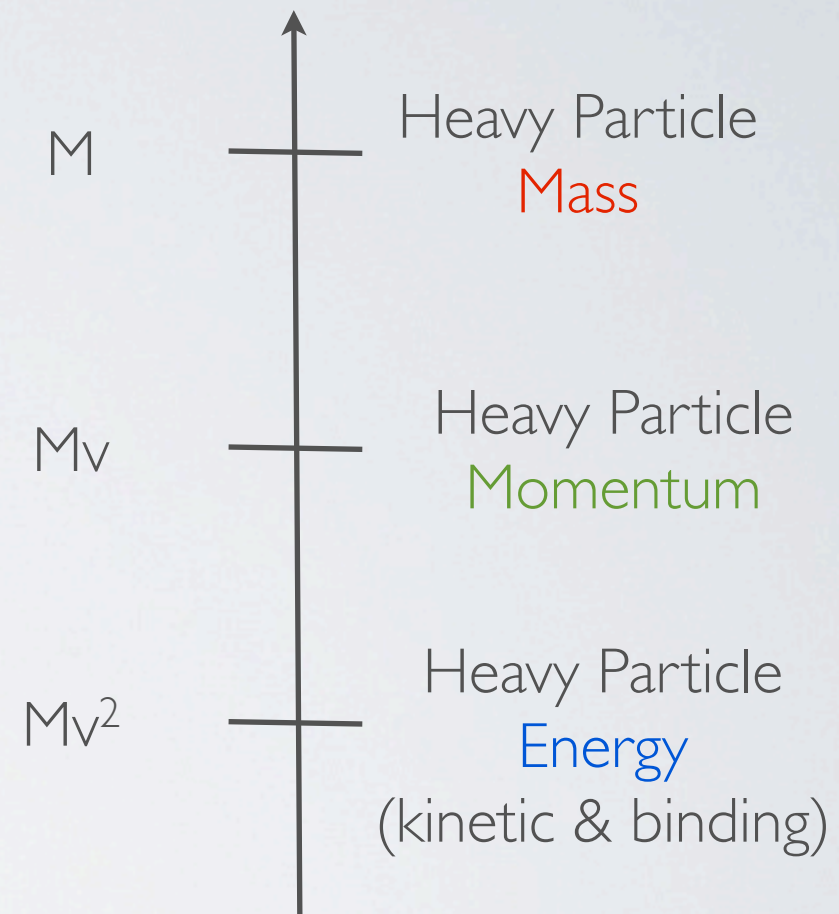
- We can use Renormalization Group to resum kinematic logs



Integrate out hard gauge boson modes, but keep those **collinear** to null directions and **soft** fields

NR“QCD” FOR WIMPS

- **Nonrelativistic EFTs** handle separation of scales in bound-state problems*
- **Unsuppressed ladder-exchange** of potential bosons ($E \sim Mv^2$, $p \sim Mv$) \rightarrow **Sommerfeld**
- **WIMPs heavy**, but Renormalization Group **resums soft-scale logs**



Hierarchy of scales for nonrelativistic particles interacting with potential

*Classic treatment of NRQCD in Bodwin, Braaten, LePage
hep-ph/9407339

MODES & FACTORIZATION

- Large logs \rightarrow disparate scales ($\lambda \sim m_W/M_{\text{wimp}}$) \rightarrow factorization
- Factorization lets us separate 2 nontrivial behaviors (Sommerfeld and Sudakov) in hybrid NRQCD/SCET theory*
- Setting up EFT requires list of relevant modes

WIMPs (χ) : ($E \sim \lambda^2$, $p \sim \lambda$)

Potential: ($E \sim \lambda^2$, $p \sim \lambda$)

Collinear ($B^{\mu\perp}$) : ($k_+ \sim 1$, $k_- \sim \lambda^2$, $k_\perp \sim \lambda$)

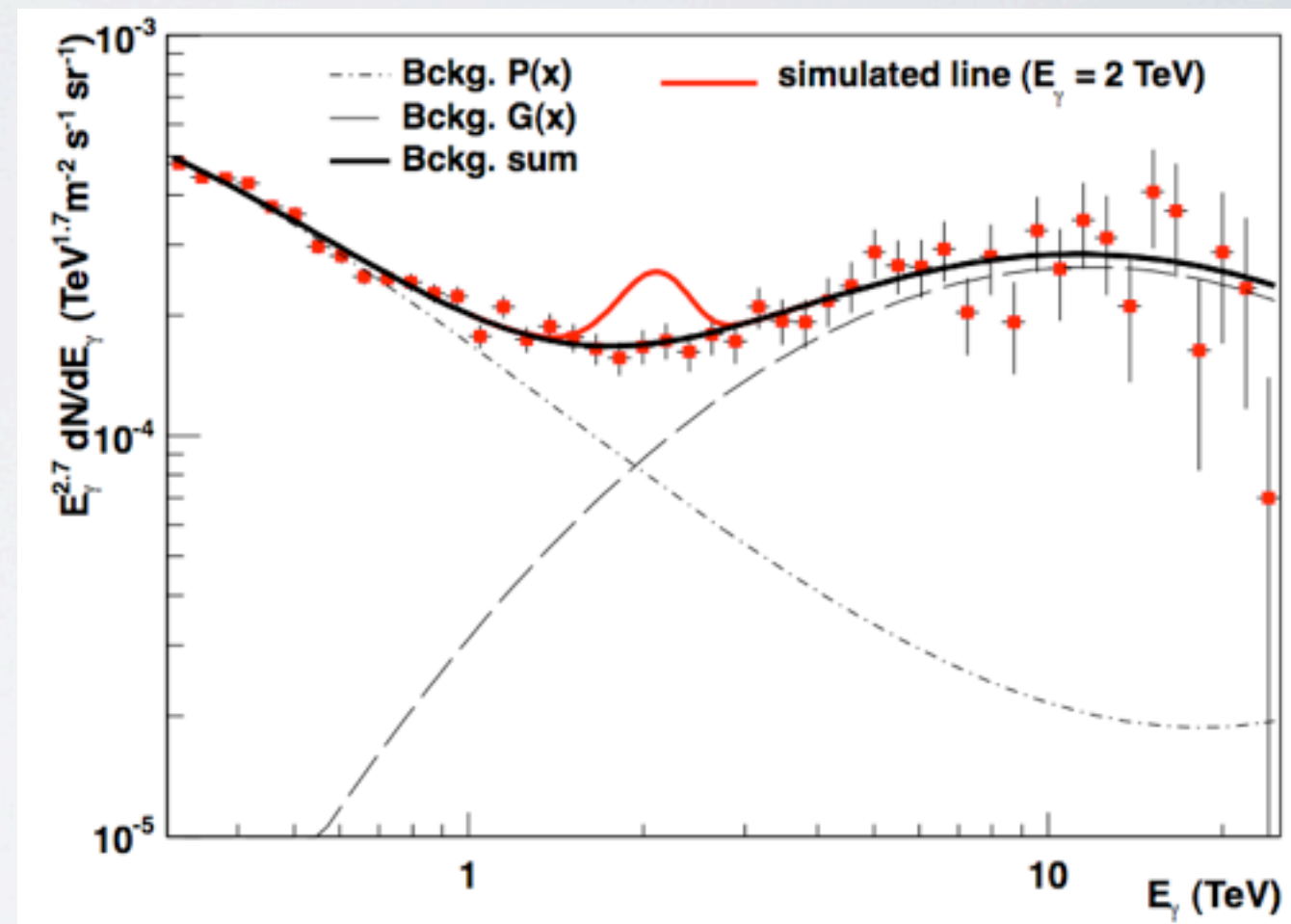
Soft (S_{ab}) : ($k_+ \sim \lambda$, $k_- \sim \lambda$, $k_\perp \sim \lambda$)

These are all
just W field in
full theory

*See also Fleming, Leibovich, Mehen hep-ph/0607121
for photon spectrum for quarkonium decays

SEMI-INCLUSIVE ANNIHILATION

- Our interest is in setting limits from indirect detection
- HESS is an air Cherenkov telescope that observes photons colliding with the atmosphere
- Therefore, we compute $XX \rightarrow Y + X$



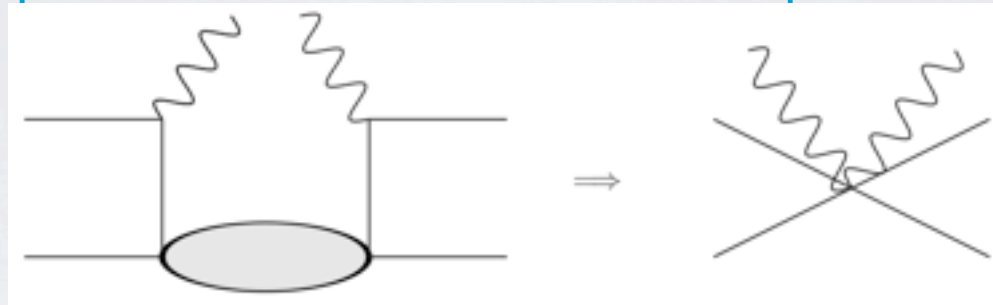
From HESS collaboration 1301.1173
at 3 TeV, energy resolution is $\sim 400 \text{ GeV}$

$$E_\gamma (\text{soft } W) = M_X - m_W/2$$

$$E_\gamma (\text{collinear } Ws) = M_X - m_W^2/M_X$$

OPERATOR BASIS

- Since our interest is **semi-inclusive processes**, it is useful to work with the **Operator Product Expansion (OPE)**



- Matching **tree level with one-loop running**, we generate:

$$O_1 = (\bar{\chi}\gamma^5\chi) |0\rangle\langle 0| (\bar{\chi}\gamma^5\chi) B^{\mu A\perp} B_{\mu}^{A\perp}$$

$$O_2 = \frac{1}{2} \left\{ (\bar{\chi}\gamma^5\chi) |0\rangle\langle 0| (\bar{\chi}_A\gamma^5\chi_B) + (\bar{\chi}_A\gamma^5\chi_B) |0\rangle\langle 0| (\bar{\chi}\gamma^5\chi) \right\} B_{\mu}^{\perp A} B^{\mu B\perp}$$

$$O_3 = (\bar{\chi}_C\gamma^5\chi_D) |0\rangle\langle 0| (\bar{\chi}_D\gamma^5\chi_C) B^{\mu A\perp} B_{\mu}^{A\perp}$$

$$O_4 = (\bar{\chi}_A\gamma^5\chi_C) |0\rangle\langle 0| (\bar{\chi}_C\gamma^5\chi_B) B_{\mu}^{\perp A} B^{\mu B\perp}$$

Vacuum projectors for WIMPs guarantee large momentum in process needed for OPE

We implicitly work with SU(2) adjoint, so basis reduced by having Majorana fermion

Spin-singlets by Fermi statistics up to $\mathcal{O}(v)$ corrections

Collinear boson fields in symmetric limit

WILSON COEFFICIENTS

- We have **four operators**, but controlled by **one tree-level matching coefficient**
- Just **two dimension-five operators** in “square root” of OPE, $\mathbf{X}\mathbf{X}B_nB_{\bar{n}}$ and $\mathbf{X}^C\mathbf{X}^D B_n^C B_{\bar{n}}^D$ and
- Their **coefficients equal and opposite** to cancel, e.g.
 $\mathbf{X}^3\mathbf{X}^3 \rightarrow W^3W^3$
- Squaring in OPE gives trivial color contraction, so

$$\begin{aligned} C_1 &\equiv C & C_2 &= -2C \\ C_3 &= 0 & C_4 &= C \end{aligned}$$

$$C(M_\chi) = \frac{\pi\alpha_W^2 \sin^2 \theta_W}{2M_\chi^3}$$

ANOMALOUS DIMENSION RESULTS

- For the collinear and soft sectors of our operators, (a - nonsinglet and b - singlet)

$$\gamma_{aa}^c = \frac{3g^2}{4\pi^2} \log\left(\frac{\nu^2}{4M_\chi^2}\right), \quad \gamma_{aa}^s = \frac{-3g^2}{4\pi^2} \log\left(\frac{\nu^2}{\mu^2}\right),$$

$$\gamma_{ba}^c = \frac{-g^2}{4\pi^2} \log\left(\frac{\nu^2}{4M_\chi^2}\right), \quad \gamma_{ba}^s = \frac{g^2}{4\pi^2} \log\left(\frac{\nu^2}{\mu^2}\right)$$

Note ν dependence drops out in soft-collinear sum

- Resum logs from Renormalization Group equation (2,4 - nonsinglet and 1,3 - singlet)

$$\mu \frac{d}{d\mu} C_{2,4}(\mu) = -(\gamma_{aa}^c + \gamma_{aa}^s) C_{2,4}$$

$$\mu \frac{d}{d\mu} C_{1,3}(\mu) = -(\gamma_{ba}^c + \gamma_{ba}^s) C_{2,4}.$$

Logs minimized for (μ, ν)
 soft: (m_W, m_W)
 collinear: (M_χ, m_W)

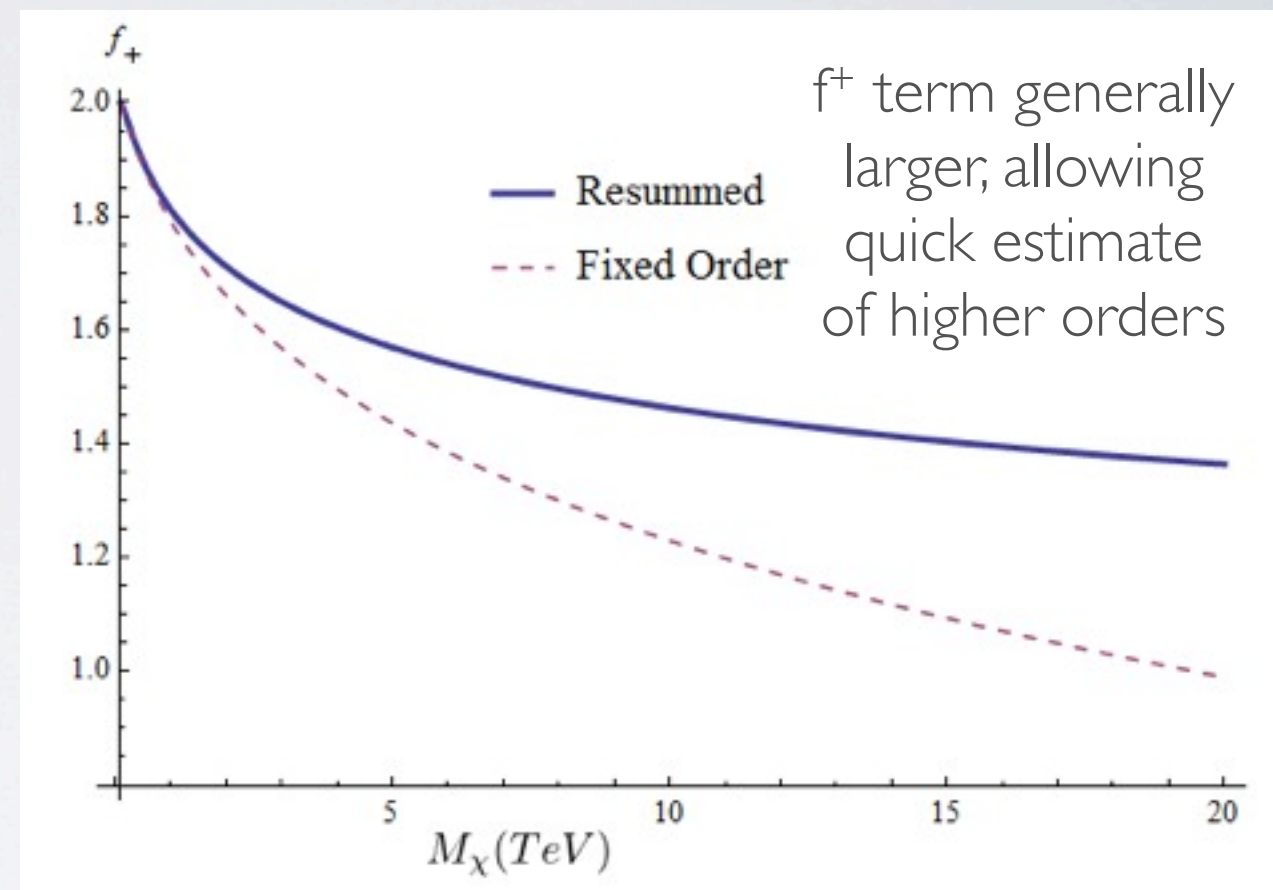
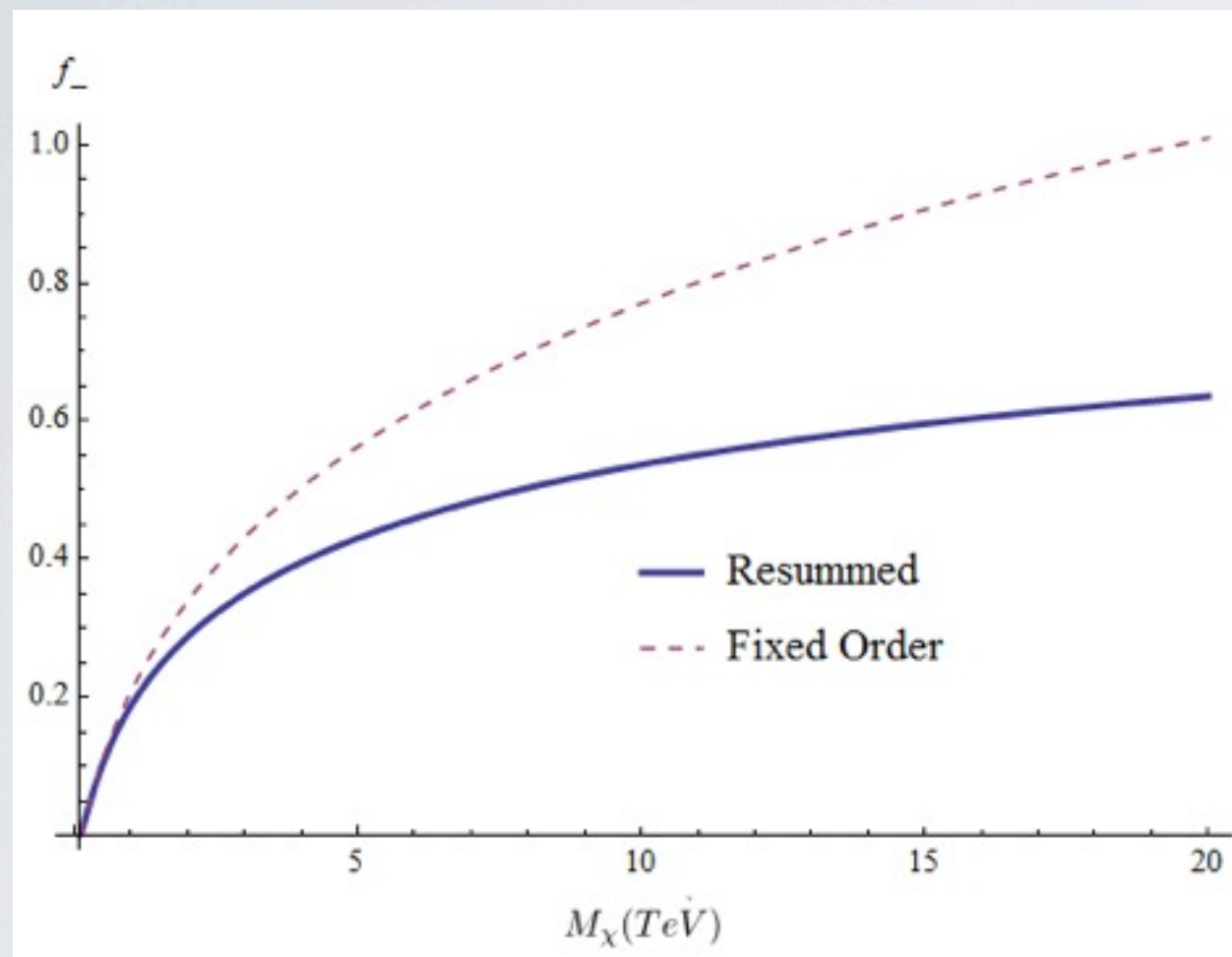
TOTAL RATE

$$\frac{1}{E_\gamma} \frac{d\sigma}{dE_\gamma} = \frac{C_1(\mu = E_\gamma)}{4M_\chi^2 v} \delta(E_\gamma - M_\chi) \left[\frac{2}{3} f_- |\psi_{00}(0)|^2 + 2f_+ |\psi_{+-}(0)|^2 + \frac{2}{3} f_- (\psi_{00}\psi_{+-} + \text{h.c.}) \right]$$

- The **ψ -factors** quantify the **Sommerfeld** enhancement for annihilating state
- The **f-factors** arise from running Wilson coefficients and resum **Sudakov** double-logs

$$f_\pm \equiv 1 \pm \exp\left[-\frac{3\alpha_W}{\pi} \log^2\left(\frac{M_W}{E_\gamma}\right)\right]$$

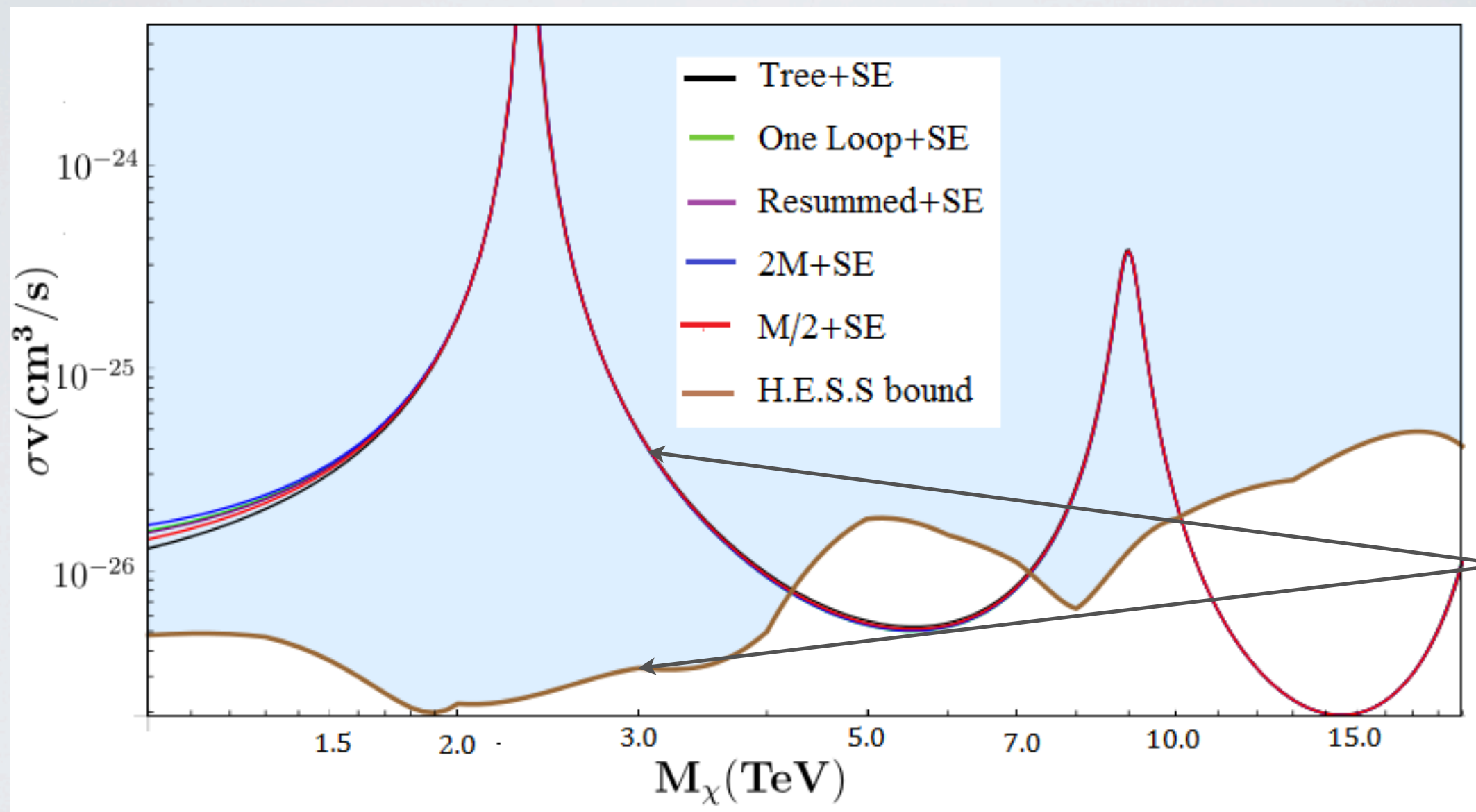
RESUMMATION



Sudakov factor vs. Dark Matter mass
Resummation is modest $\sim 5\%$ affect for thermal Wino (3 TeV)

More important effect that we looked at semi-inclusive instead of two-body annihilation

TOTAL RATE & EXCLUSION

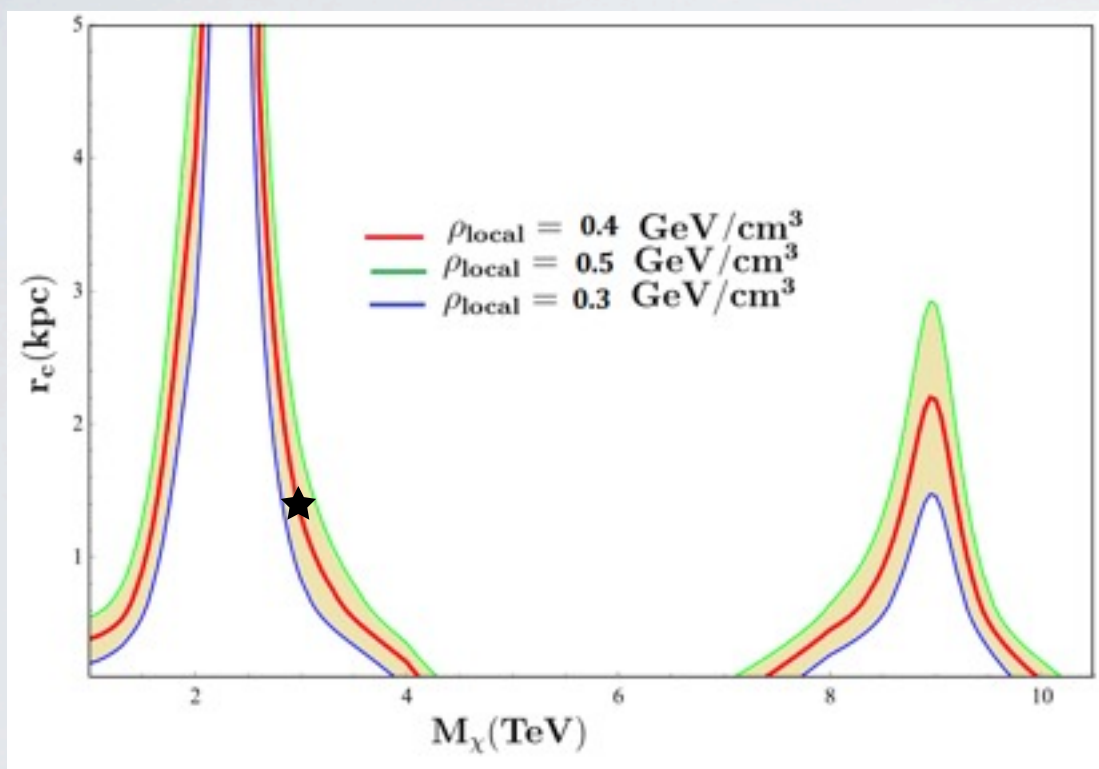


Wino escape
at higher orders
foiled by more
accurate
calculation

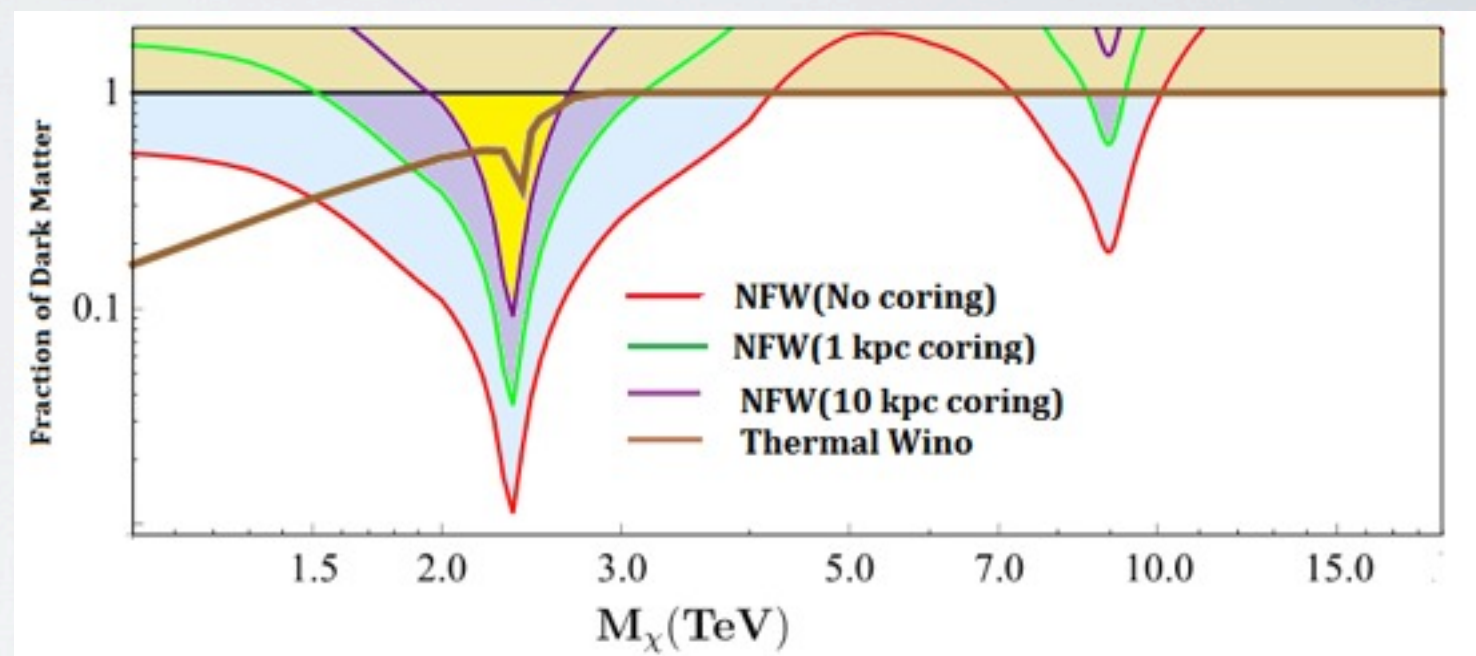
Exclusion curve taken from Ovanesyan, Slatyer, and Stewart (1409.8294); HESS data with NFW profile

WINO VIABILITY

Initial motivation for Wino stressed its simplicity,
but perhaps its role in Dark Matter is **more involved**, including
a **non-thermal history**, **multi-component DM**, **mixing** with other EW states



Imposing a constant density below
a given radius for NFW (core),
at what point does wino
become viable total DM?



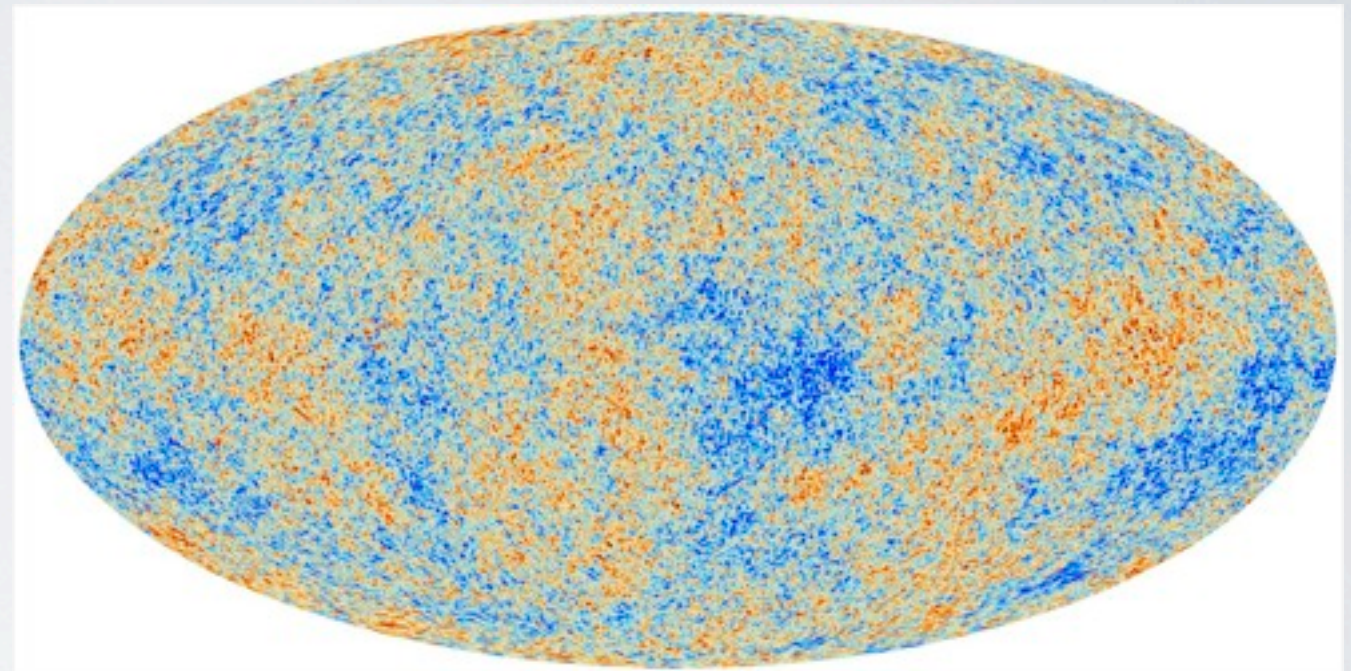
Possibility for the wino to make up **some fraction**
of DM with NFW profile flattened to a
constant core at some radius

WINO CONCLUSION

- When computing observationally relevant semi-inclusive rate, NLO effects are small (\sim few%) compared to \sim 50% found in exclusive analyses: Ovanesyan et al. (1409.8294); Bauer et al. (1409.7392)
 - Semi-Inclusive \rightarrow Leading Log operator mixing $\rightarrow 1 + \text{Exp}[-\text{Log}^2]$.
Exclusive calculation \rightarrow no mixing \rightarrow simply $\text{Exp}[-\text{Log}^2]$
- Viability of thermal wino dark matter requires profile in tension with simulation (core \sim 1.5 kpc)
- Discovery of wino would have huge implications for astrophysical Dark Matter

THE RUTHLESS HUNT FOR NEW PHYSICS

- Understanding TeV-scale would be a great triumph of science
 - Electroweak symmetry breaking
 - WIMP dark matter
- Q: Is that enough?



A: Would the rich like to be richer?

- To understand physics at $M \gg \text{TeV}$, we will need the **particle accelerator universe** → observables of inflation

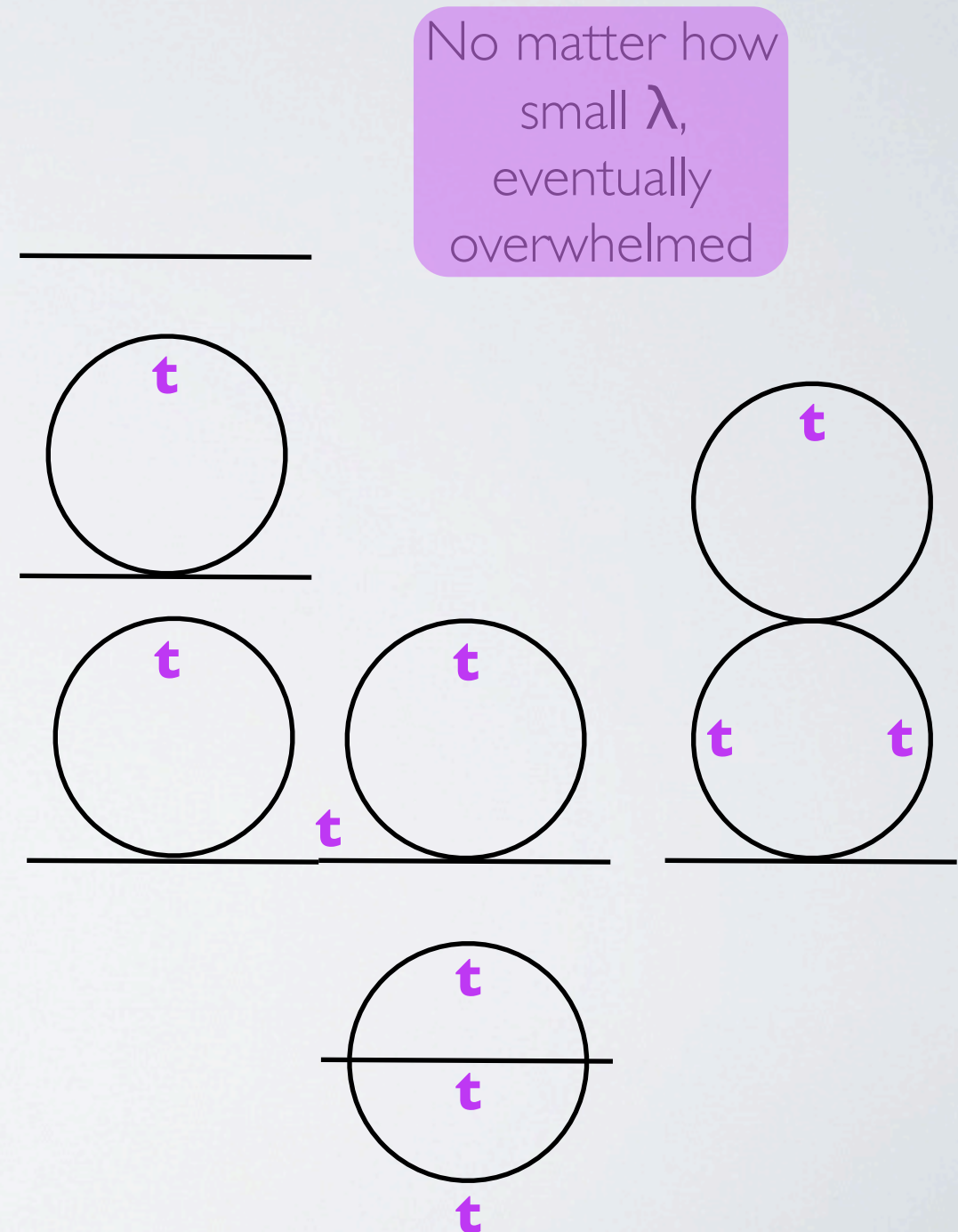
Temperature anisotropy map from Planck satellite
Experiment confirms nearly $1/k^3$
power spectrum expected from a quasi-De Sitter geometry,

UNDERSTANDING PERTURBATION THEORY IN DE SITTER

- In 1940s and 1950s, theorists worked to **understand QED to all orders** → Deep insight into Renormalization Group
- Inflation successful, but it raises **conceptual problems**, what is grammar for QM on cosmological scales?
- For clues, use pure **DS as theoretical laboratory** massless field contains IR pathology
- Can regulate IR, but at cost of **linear-in-t growth** of propagator

$$\langle \phi_k \phi_{-k} \rangle \sim \frac{H^2(1 + k^2 \eta^2)}{k^3} \quad \langle \phi(x) \phi(y) \rangle \sim \int \frac{dk}{k} \sim \log(k_{UV}) - \log(k_{IR})$$

$$\langle \phi(x) \phi(y) \rangle \sim H^2 \log(a = e^{Ht}) = H^3 t$$



IR OF DE SITTER \leftrightarrow IR OF QCD

- Just as in gauge theory (QCD, electroweak), we have **poorly behaved infrared**
- Problem demands novel EFT methods, but morally similar to SCET, divide field into modes, **carefully treat IR and resum**

$$\begin{aligned} \psi[\{\phi_1\}; t + \Delta t]_{IR} = & \psi_{BD, Ha' > k > Ha}[\phi_{1k}, t + \Delta t] \longleftarrow \text{Modes redshift from perturbative UV} \\ & \times \int \mathcal{D}\phi_{0q} \text{ "}\delta[\phi_{0q} - \phi_{cl}(\phi_{1q}; t, t + \Delta t)]\text{"} \longleftarrow \text{Soft modes obey first-order stationary phase approximation} \\ & \times \psi_{\text{soft}}[\{\phi_{0q}\}; t] e^{iS_{\text{soft}, cl}[\phi_{1q}, \phi_{0q}; t, t + \Delta t]} \end{aligned}$$

- Update equation for wavefunctional in path integral gives **simple evolution for wavefunctional mod-squared**:*

$$\dot{p}(\phi, t) = \frac{1}{3H} \partial_\phi [V'(\phi) p(\phi, t)] + \frac{H^3}{8\pi^2} \partial_\phi^2 p(\phi, t)$$

$$p(\phi, t) = N e^{-\frac{8\pi^2}{3H^4} V} + \sum_{n=1}^{\infty} \Phi_n(\phi) e^{-\Gamma_n t}$$

- DS/Parton Shower correspondence? Leading IR physics takes us to: Markovian evolution, flow equation, UV fixed point...

*MB and R. Sundrum 1503.xxxxxx
 "Stochastic Inflation" Starobinsky (1986)

EFFECTIVE FIELD THEORY UNIVERSE

- Effective Field Theory can simply mean integrating out heavy particles and is useful for parametrizing Beyond the Standard Model physics

MB: 0706.1380 (dimension-6 operators in deconstructed, composite Higgs Models)
MB & B.Tweedie: 1212.4888: (top quark spin observables for higher-dimension operators)
J.Adelman et al.: 1308.5274: (top quark rate observables for higher-dimension operators)

- EFT is much richer formalism to understand wide variety of systems with intrinsic scale hierarchies (jets from hard collisions, bound states, long-lived inflationary universe), often involving the same field

MB, C. Marcantonini, & I. Stewart: 1007.0758 (NLL parton shower from SCET)
MB & A. Katz: 1204.6032 (Higgs decays via new physics to NRQCD bound states)
MB et al.: 1406.2295 (NRQCD bound states in jets analyzed with SCET to understand quarkonium polarization puzzle)
MB, I. Rothstein & V.Vaidya: 1409.4415 (SCET+NRQCD formalism to resum wino annihilation logs)
MB, I. Rothstein & V.Vaidya: 1409.8696 (SCET+NRQCD calculation of wino annihilation rate)
MB & R. Sundrum: 1503.xxxxx (Resummation of time for light scalars in DS)

- Pushing ever-forward in energy, understanding disparate-scale systems will be crucial to answering our deepest questions.**

Top and other heavy particle
observables, including spin
Irrelevant operator analysis of new models

Resumming electroweak logs at colliders
Seeing color of partons in jets
Identifying Dark Matter
Understanding Quantum Field Theory in De Sitter

SUSY & DARK MATTER

- The Minimal Supersymmetric Standard Model (MSSM) comes with several natural WIMP dark matter candidates
 - Bino: Generic LSP in many SUSY-breaking scenarios. Overcloses universe unless nearly degenerate slepton provides co-annihilation ($\Delta M/M \sim 5\%$)
 - Wino: Generic LSP in Anomaly Mediated Supersymmetry Breaking (AMSB)
 - Higgsino: Pure Higgsino ruled out by direct detection, but bino/wino admixture possible*
 - Sneutrino: Ruled out by direct detection, but could be possible in extension
 - Gravitino: LSP of low-scale Gauge Mediation, very light $O(100 \text{ keV})$, with overclosure and Big Bang Nucleosynthesis problems

*See “The Well-Tempered Neutralino” Arkani-Hamed et al. hep-ph/0601041

WILSON LINES, GAUGE INVARIANCE, SOFTS

- SCET has **rich gauge structure** (separate for soft and collinear sectors) and collinear fields contain **implicit collinear Wilson lines**

$$B_{\mu}^{a\perp} \equiv f^{abc} W_n^T (D_{\mu}^{\perp})^{bc} W_n$$

- We have **soft Wilson lines** for both WIMP and collinear fields

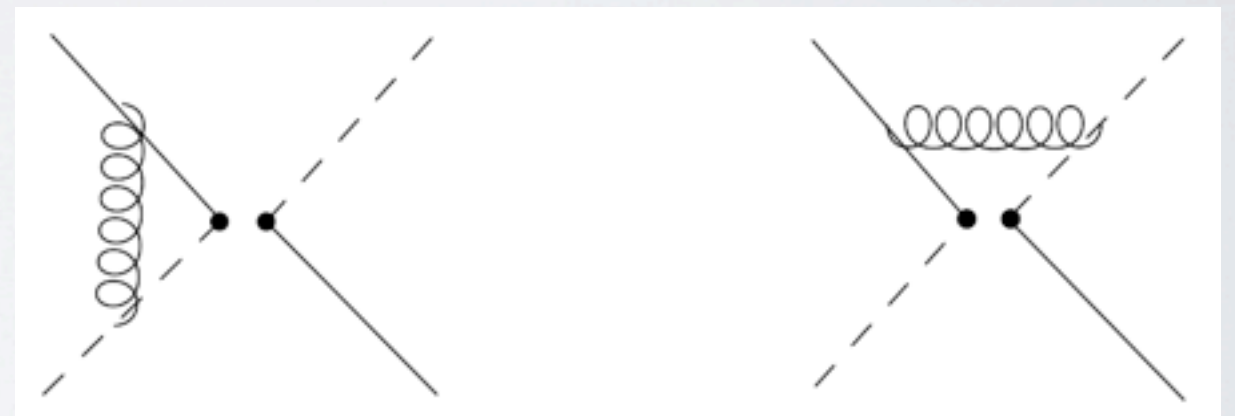
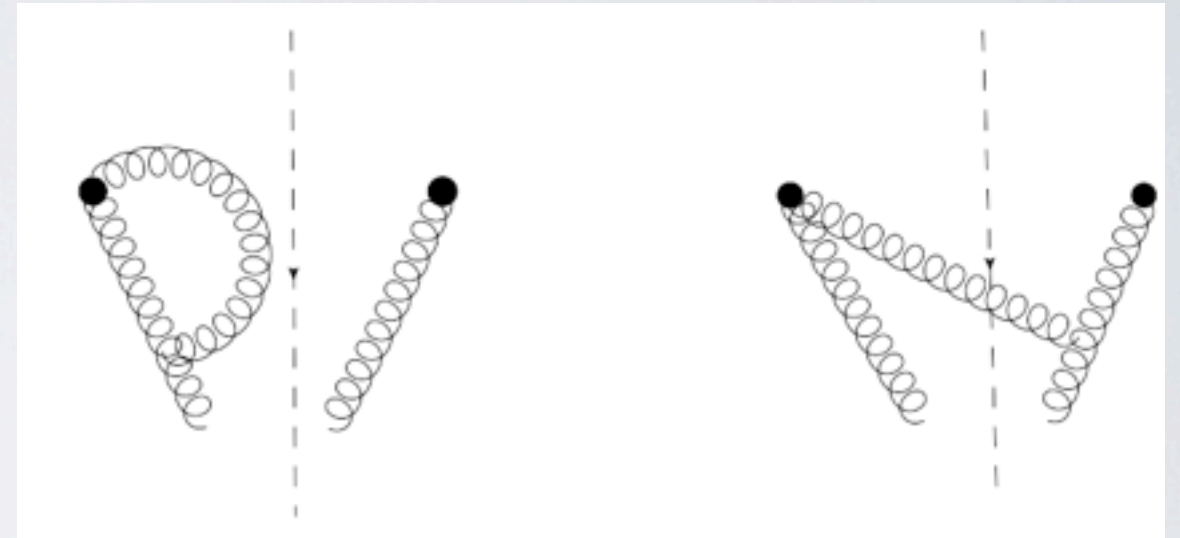
$$S_{(v,n)} = P[e^{ig \int_{-\infty}^0 (v,n) \cdot A((v,n)\lambda) d\lambda}]$$

- Soft&Collinear-gauge-boson structure is therefore

$$\begin{aligned} O_s^a &= S_{vA'A}^T S_{vBB'} S_{n\tilde{A}A}^T S_{nB\tilde{B}} & O_s^b &= \mathbf{1} \delta_{\tilde{A}\tilde{B}} \delta_{A'B'} \\ O_c^a &= B_{\tilde{A}}^{\perp} B_{\tilde{B}}^{\perp} & O_c^b &= B^{\perp} \cdot B^{\perp} \delta_{\tilde{A}\tilde{B}} \end{aligned}$$

ANOMALOUS DIMENSIONS

- Compute **soft & collinear anomalous dimensions** separately
- OPE converts amplitude-squared to operator whose **expectation value gives rate**
- Thus, **real & virtual corrections** to $XX \rightarrow Y + X$ will appear as **loops**



Above: **Collinear** contributions O_c^a (real & virtual)

Below: Interactions between **soft Wilson lines** O_s^a (solid - timelike; dashed - lightlike) $O_{c,s}^b$ has **trivial** color structure and thus **0-anomalous dimension**

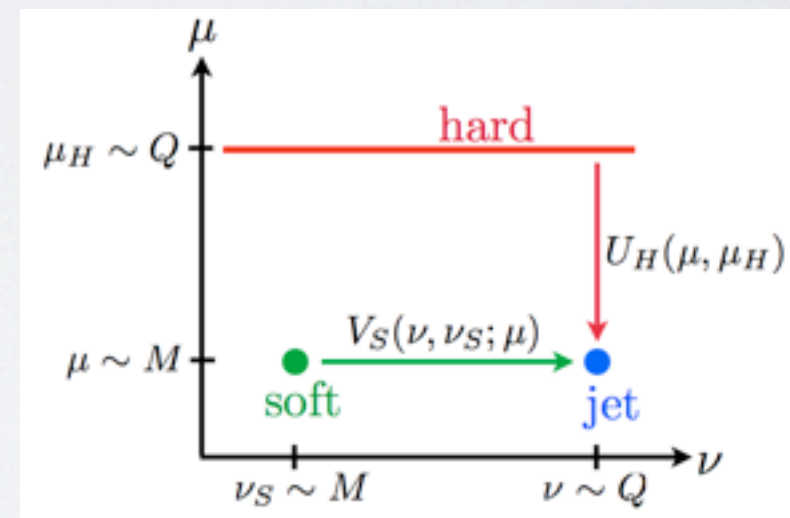
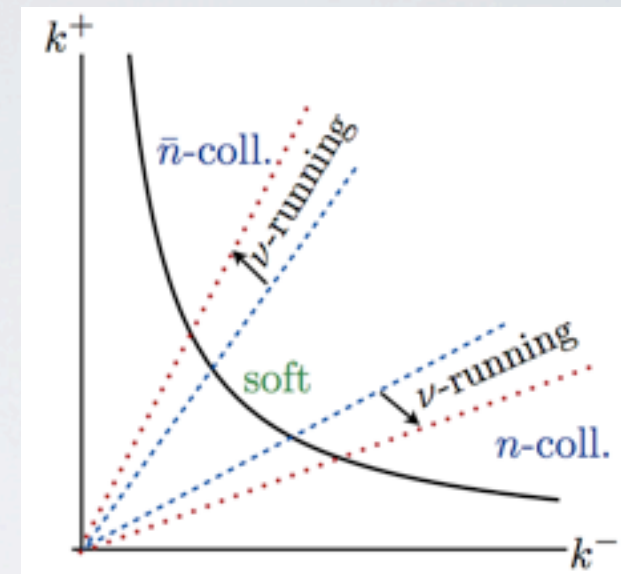
RAPIDITY RG

- SCET is a “modal” theory

$$A_\mu = A_\mu^{c,n} + A_\mu^{c,\bar{n}} + A_\mu^{soft} + \dots$$

- We can get **divergences** when integrals invade other sectors. Soft-collinear overlap requires **boost-violating regulator**
- Regulating sets up **RG** for **resumming** these rapidity logs

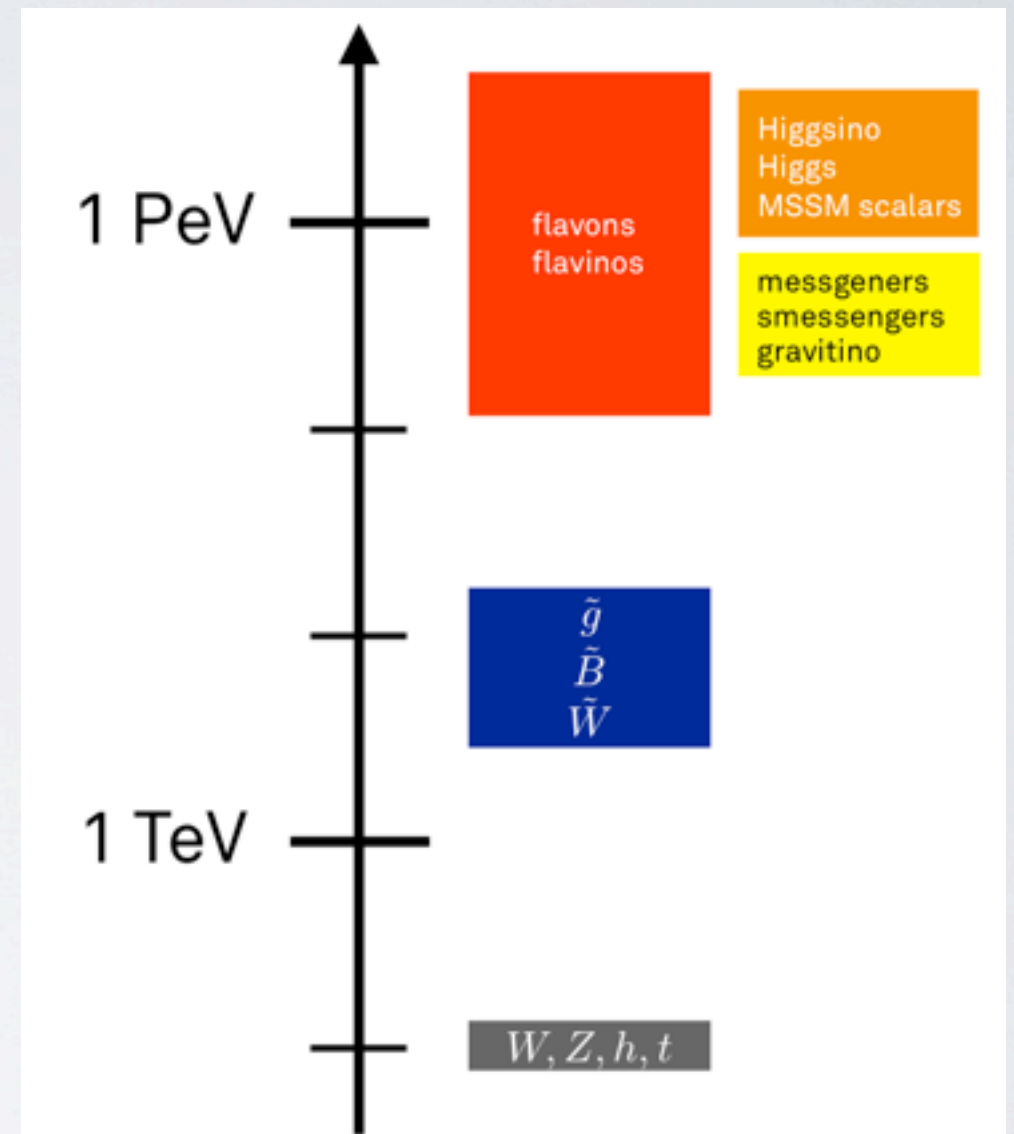
$$W_n = \sum_{\text{perms}} \exp \left[-\frac{g}{\bar{n} \cdot P} \frac{\nu^\eta}{|\bar{n} \cdot P|^\eta} \bar{n} \cdot A_n \right]$$



From Chiu et al. [202.0814]: In SCETII, **soft and collinear modes have same virtuality**
v-running lets us **minimize log** between **soft & collinear scales**

POST-HIGGS SUSY

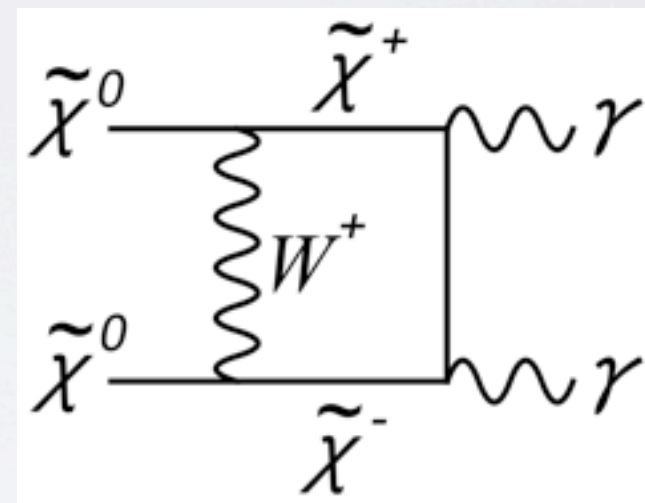
- For all its virtues, SUSY is famously unobserved
- Higgs + nothing else means?
 - SUSY to eliminate most fine-tuning? 10^{-8} instead of 10^{-32}
 - Higgs mass ($125 \text{ GeV} > m_Z$) and flavor physics point to sfermions at 100-1000 TeV
 - Simpler SUSY model building (Gravity + Anomaly mediation)
 - Gauginos (w/ wino LSP) at right scale for WIMP Miracle



From 1403.6118: MB, Stolarski, and Zorawski
 Mini-split SUSY allows a radiative generation
 of flavor hierarchies
 and allows for thermal WIMP-DM

CHARGED & NEUTRAL STATES

- Perturbative annihilation proceeds through either **charged (tree)** or **neutral (one-loop)** channels



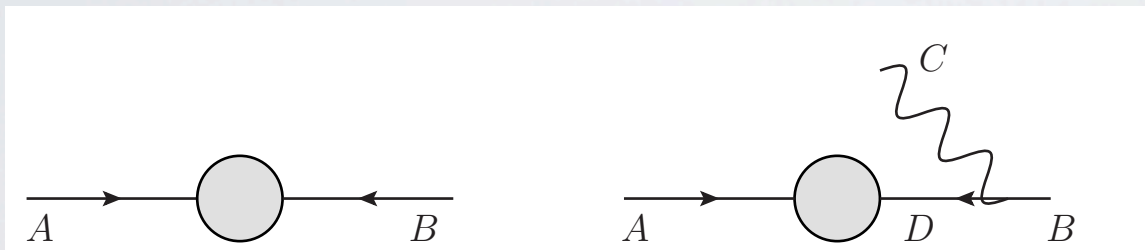
$$\sigma_{\text{one-loop}} v = \frac{4\pi\alpha^2\alpha_W^2}{m_W^2}$$

- For **asymptotic neutral state** (Dark Matter), we compute amplitude for charged or neutral state at origin

$$\begin{aligned}\psi_{00} &= \langle 0 | \bar{\chi}^0 \gamma^5 \chi^0 | \chi^0 \chi^0 \rangle_S \\ \psi_{\pm} &= \langle 0 | \bar{\chi}^{\pm} \gamma^5 \chi^{\pm} | \chi^0 \chi^0 \rangle_S\end{aligned}$$

BLOCH-NORDSIECK THEOREM VIOLATION*

- Electroweak physics has **infrared divergences**, even in **fully inclusive** observables



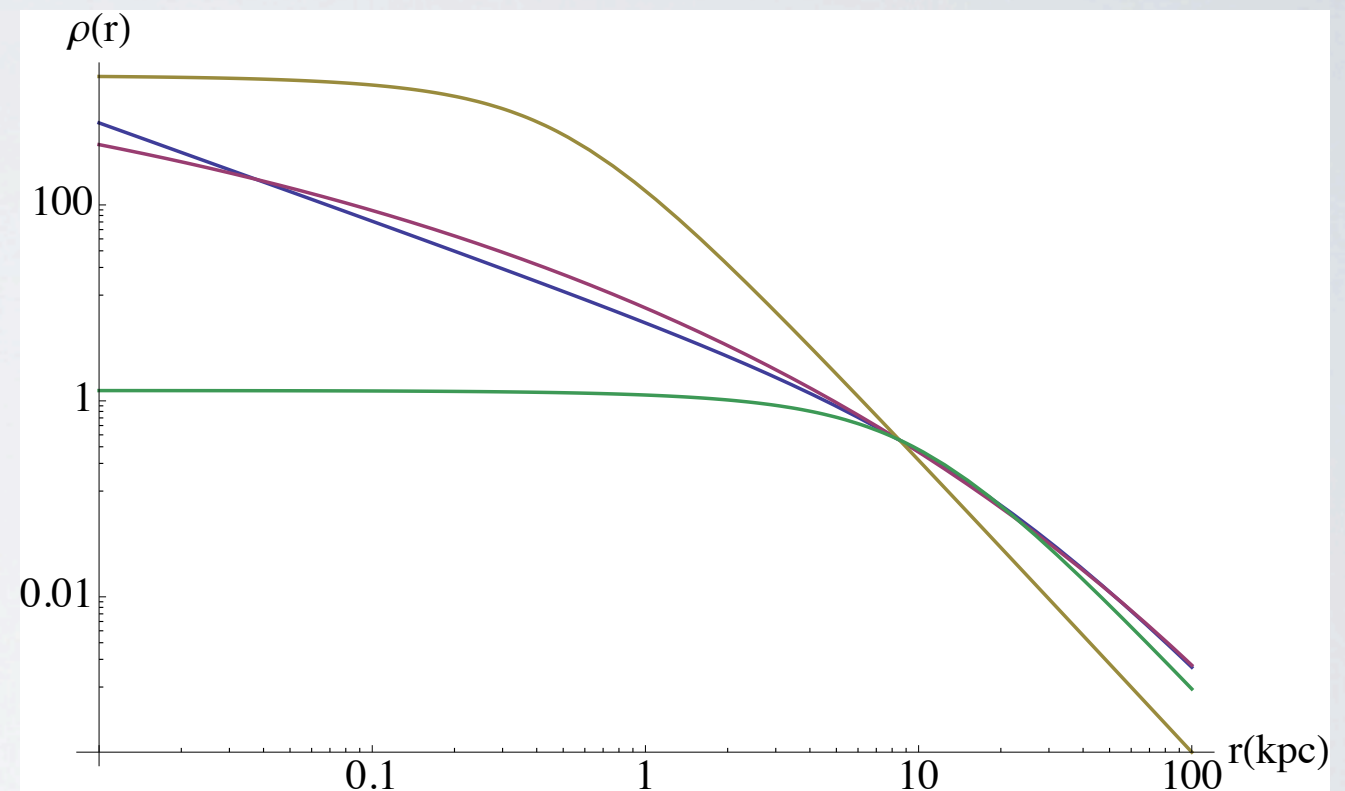
$\sigma_{AB} \neq \sigma_{AD}$, virtual
corrections only cancel
emission upon color averaging

- We avoid pathology because
 - QED**: Emission doesn't change particle identity \rightarrow real/virtual cancellation \rightarrow Bloch-Nordsieck
 - QCD**: Singlets let us **average over initial colors**, factorization isolates IR sensitivity (e.g. PDFs)
 - Electroweak**: Gauge boson masses cut off divergence, but allow for $\log(Q^2/m_W^2)^2$

THE HALO LOOPHOLE

- Indirect detection searches suffer from large astrophysical uncertainties from unknown form of DM halo.
- Observation only constrains possible core < 10 kpc (Nesti & Salucci 1304.5127)
- Flux of photons observed by HESS proportional to integrated ρ^2
- Dwarf galaxies evince corings, but simulation, even with baryons, finds cusps down to 1 kpc*

*1208.4844, 1305.5360, 1306.0898



Blue (NFW), Red (Einasto),
Yellow (Burkert-0.5), Green (Burkert-10)
fixed to local density (8.5 kpc)
of 0.4 GeV/cm³

$$\rho_{\text{NFW}}(r) = \frac{\rho_0}{(r/20\text{kpc})(1 + r/20\text{kpc})^2}$$

$$\rho_{\text{Burk.}}(r) = \frac{\rho_0}{(1 + r/r_c)(1 + r/r_c)^2}$$