## **DEPARTMENT OF ECONOMICS**

### **Working Paper**

Theoretical and empirical shortcomings of the Kaleckian investment function

by

Peter Skott

Working Paper 2008-11 Revised version, December 2009



# UNIVERSITY OF MASSACHUSETTS AMHERST

## Theoretical and empirical shortcomings of the Kaleckian investment function\*

#### Peter Skott

4th December 2009

#### Abstract

The specification of the accumulation function is critical for the properties and implications of structuralist and post-Keynesian growth models, and a large Kaleckian literature extends the standard short-run "Keynesian stability condition" to the long run by assuming that long-run accumulation is relatively insensitive to variations in the utilization rate of capital. The Kaleckian position has been defended by Dutt and Lavoie, among others. This paper examines the defense and finds it unconvincing: the Kaleckian specification of the accumulation function is behaviorally implausible and lacks empirical support.

JEL classification: E12, E32

Key words: Kalecki, Harrod, investment function, stability, post keynesian theory, utilization rate, excess capacity

<sup>\*</sup>I thank Fabian Slonimczyk for excellent research assistance. Paul Auerbach, Amitava Dutt, Alexander Julius, Marc Lavoie, Ben Zipperer and participants in the Eastern Economic Association Meetings, March 2008, and the Analytical Political Economy Workshop, Queen Mary University London, May 2008, provided helpful comments on an early draft.

#### 1 Introduction

A few years ago Steedman (1992) posed a number of "Questions for Kaleckians". This paper also raises questions for Kaleckians. The questions, however, are different.

Steedman's main concern was aggregation and the use of representative, vertically integrated firms. Steedman's point is correct - aggregates sometimes behave in ways that one might not expect on the basis of an analysis of representative agents - but complete disaggregation, like full 'generality' or 'realism', is unattainable. Aggregation is necessary, and one must choose the appropriate degree of aggregation, given the questions at hand.

In this paper, I shall assume that aggregational problems do not undermine the standard one-sector assumption that characterizes Kaleckian macroeconomics (and most macroeconomic models, more generally). In other words, I shall take it for granted that we may analyze pricing, output and production decisions as if they were generated by representative firms. In fact, sectoral differences with respect to technologies, demand conditions, labor relations, or other important characteristics could easily undermine this assumption. A shift of consumption demand toward capital-intensive consumption goods, for instance, could increase aggregate investment, even without any change in aggregate consumption demand. The possible scenarios and complications are legion but in the absence of any information about the direction of any such effects, aggregate macroeconomic models may provide a useful benchmark. Kaleckian models of growth and distribution, however, have other weaknesses, weaknesses that are specific to this particular branch of macro theory. The Kaleckian investment function, in particular, is hard to justify.

Contemporary mainstream macroeconomics shows little interest in investment functions, at least compared to the outpouring of work on the investment functions from the 1950s to the 1980s. In some ways this is not surprising. The earlier literature on investment failed to produce clear empirical results, and 'primitive' equations in many cases performed as well as more 'sophisticated' specifications that included cost-of-capital variables or Tobin's q. From a theoretical perspective, moreover, aggregate investment is no longer central. A traditional Keynesian approach regarded investment as a key influence on aggregate demand and employment, and as the main mover of the business cycle. Contemporary New-Classical and New-Keynesian theory has a different perspective. Employment may deviate from the natural rate (or NAIRU) in the short run but nominal and real rigidities, mainly relating to the labor market, are seen as the key to an understanding of these deviations, and business cycles are modeled in the Frisch-tradition as the result of propagation mechanisms playing on exogenous shocks, rather than as being generated endogenously by multiplier/accelerator mechanisms. With the level of output and employment largely determined by the labor market - certainly in the medium run and consumption modeled in terms of intertemporally optimizing households, there is no

<sup>&</sup>lt;sup>1</sup>It is striking that Caballero (1999) discusses equilibrium interactions and lumpiness in investment, giving great attention to signalling complementaries but without even raising the question of aggregate demand.

real need for (nor indeed, much room for) a separate aggregate investment function.

Having said this, contemporary investment theory appears to agree on a basic stock adjustment principle: investment is the result of firms trying to adjust their capital stock toward some desired level,  $K^*$ . Differences arise over the determination of the desired stock and the reasons for gradual adjustment. Firms' objectives may be profit maximization but sales or growth also enter the objective function sometimes. More important differences arise from the treatment of the constraints: simple accelerator models assume a fixed-coefficient production function and adaptive expectations; "neoclassical" theories include cost-of-capital variables to capture a choice of technique; q-theories look for measurable variables that capture expectations of future returns to investment relative to the cost of capital; cash-flow variables may become important as the result of credit market imperfections; profound uncertainty may render formal optimization models largely irrelevant; adjustment costs may or may not be convex.

In this paper I deliberately abstract from these and other complications. I shall assume that (i) firms try to maximize profits, (ii) there is a fixed-coefficient production function, (iii) the availability of financing does not constrain investment. Moreover, since the main focus of the paper is on the medium and long run, the nature of adjustment costs is of little importance.

The first two assumptions are almost universal in both the Kaleckian and the broader post-Keynesian literature. Post-Keynesian theories by and large ignore the choice of technique and typically assume a fixed-coefficient production function.<sup>2</sup> The output-capital ratio, nevertheless, need not be exogenously given. Investment is irreversible and in the short run utilization rates depend on aggregate demand.

The Kaleckian model extends the short-run variability of utilization rates to the medium and long run and implies that permanent shocks to aggregate demand - a change in saving rates, for instance - can lead to permanent and quantitatively significant changes in utilization. This paper challenges the Kaleckian approach. I shall argue (i) that there are good theoretical reasons to rule out steady-growth deviations between actual and desired utilization rates, (ii) that the theoretical case for (quantitatively significant) adaptive changes in desired utilization is weak, (iii) that the Kaleckian specification implies long-run variations in utilization rates that have no counterpart in the data, and (iv) that existing econometric studies have been badly misinterpreted.

Section 2 considers the theoretical argument. It outlines a canonical Kaleckian model and a Harrodian alternative, and then briefly summarizes some of the debates surrounding the Kaleckian accumulation function. Section 3 examines two defenses of the Kaleckian position in greater detail. One defense, suggested by Lavoie (1995), Amadeo (1986) and Dutt (1997), accepts the consistency between desired and actual utilization in a long-run equilibrium but focuses on endogenous changes in the desired (or 'normal') rate; another defense, elaborated by Dallery and van Treeck (2008), explains long-run discrepancies between desired and actual utilization as the result of the existence of macroeconomic

<sup>&</sup>lt;sup>2</sup>See Skott (1989, chapter 5) for an exception.

constraints and competing targets. Section 4 turns to empirical evidence. The section argues that, weak as it is, the existing evidence cannot support the Kaleckian specification. Section 5 offers a few concluding remarks.

#### Different post-Keynesian models<sup>3</sup> 2

#### 2.1 The Kaleckian model

Kaleckian models - as defined in this paper - are characterized by a low sensitivity of accumulation to variations in utilization and the treatment of utilization as an accommodating variable in both the short and the long run. Thus, the steady-growth value of the utilization rate is not, as in Harrodian or Robinsonian models, tied to a structurally determined desired rate. Instead, shocks to demand (changes in saving rates, for instance) can have large, permanent effects on utilization.

The basic Kaleckian model has been extended and modified in many ways. Some extensions have introduced a government sector and an explicit analysis of policy issues (e.g. Lima and Setterfield (2008)); others add financial variables or open-economy complications (e.g. Blecker 1989, 1999; Lavoie and Godley 2001-02, Dos Santos and Zezza (2008), Hein and van Treeck 2007). The focus in this paper, however, is on the structure of the basic model and the accommodating variations in the utilization rate, and for these purposes a stripped-down model of a closed economy without public sector and without financial constraints on investment will suffice.

Algebraically, the canonical Kaleckian model is exceedingly simple:

$$\frac{1}{K} = \alpha + \beta u + \gamma r \tag{1}$$

$$\frac{I}{K} = \alpha + \beta u + \gamma r \tag{1}$$

$$\frac{S}{K} = s(\pi)u\sigma \tag{2}$$

$$\frac{I}{K} = \frac{S}{K} \tag{3}$$

$$\frac{I}{K} = \frac{S}{K} \tag{3}$$

$$r = \pi u \sigma$$
 (4)

$$\pi = \bar{\pi} \tag{5}$$

$$g = \hat{K} = \frac{I}{K} - \delta \tag{6}$$

Using standard notation, equations (1)-(2) are the investment and saving functions. Investment is increasing in utilization (u) and the profit rate (r), and the saving rate out of income  $(s(\pi))$  is an increasing function of the profit share  $(\pi)$ ;  $\sigma$  denotes the technical output-capital ratio. Equation (3) is the equilibrium condition for the product market;

<sup>&</sup>lt;sup>3</sup>This section draws on Skott (2010).

<sup>&</sup>lt;sup>4</sup>Robinson (1962) assumes that adjustments in the markup generate a normal rate of utilization in steady growth; Steindl (1952) arguably held a similar position, see Flaschel and Skott (2006).

equation (4) defines the profit rate as the product of the profit share, the utilization rate and the technical output-capital ratio. Equation (5) is the pricing equation with the profit share fixed by a markup on marginal cost, the latter assumed constant and equal to unit labor cost. Equation (6) sets the growth rate of the capital stock (q = K) equal to gross accumulation minus the rate of depreciation,  $\delta$ . All parameters are assumed positive and the Keynesian stability condition is supposed to hold,

$$\frac{\partial (I/K)}{\partial u} = \beta + \gamma \bar{\pi} \sigma < s(\bar{\pi}) \sigma = \frac{\partial (S/K)}{\partial u} \tag{7}$$

Simple manipulations of equations (1)-(6) imply that

$$u^* = \frac{\alpha}{s(\bar{\pi})\sigma - \beta - \gamma\bar{\pi}\sigma} \tag{8}$$

$$g^* = \frac{\alpha s(\bar{\pi})\sigma}{s(\bar{\pi})\sigma - \beta - \gamma \bar{\pi}\sigma} - \delta \tag{9}$$

It is readily seen that if the saving function is linear in  $\pi$  ( $s(\pi) = s\pi$ ), the stability condition (7) implies that

$$\frac{\partial u^*}{\partial \bar{\pi}} \quad < \quad 0 \tag{10}$$

$$\frac{\partial u^*}{\partial \bar{\pi}} < 0$$

$$\frac{\partial g^*}{\partial \bar{\pi}} < 0$$
(10)

Thus, the economy is both 'stagnationist' (equation (10)) and 'wage led' (equation (11)) in the terminology of Marglin and Bhaduri (1990).<sup>5</sup>

Marglin and Bhaduri challenged these implications of the model and suggested that the investment function be recast with accumulation as a function of utilization and the profit share, rather than utilization and the profit rate,

$$\frac{I}{K} = \alpha + \beta u + \gamma \pi \tag{12}$$

Using this alternative specification of the investment function, they showed that the Keynesian stability condition need not produce stagnationist and wage-led regimes. The utilization rate remains an accommodating variable, however, and the main difference between the investment functions (1) and (12) is that the sensitivity of investment to changes in utilization has been reduced, relative to the sensitivity with respect to the profit share. The non-stagnationist outcomes become possible precisely because, using (12) instead of

The canonical model need not be stagnationist if the saving function is nonlinear (or just affine,  $s(\pi) = s_0 + s\pi$  with  $s_0 > 0$ ) since in this case the 'Robinsonian stability' condition  $(\frac{\partial I}{\partial \pi} < \frac{\partial S}{\partial \pi})$  can be violated even if the 'Keynesian stability' condition  $(\frac{\partial I}{\partial u} < \frac{\partial S}{\partial u})$  is met. This point, which may have been noted in the literature, was made by Ben Zipperer in comments on an early draft of this paper.

(1), we may have  $\frac{\partial (I/K)}{\partial \bar{\pi}} > \frac{\partial (S/K)}{\partial \bar{\pi}}$ , even when the Keynesian stability condition is satisfied, something that cannot occur when the investment function is given by (1) and the saving function is linear  $(s(\pi) = s\pi)$ . Equivalently, equation (12) does not exclude the possibility that, holding constant the *rate* of profit, an increase in utilization may reduce accumulation. This is in sharp contrast to Harrodian formulations. Thus, although both the Marglin-Bhaduri formulation and the Harrodian models below may produce profit-led outcomes, the behavioral assumptions are very different, and from a Harrodian perspective the Marglin-Bhaduri specification suffers from the same problems as the original Kaleckian model.

The effect of profitability on investment has no direct bearing on the argument in this paper and to simplify the exposition  $\gamma$  is set equal to zero. In this special case, the two investment functions (1) and (12) coincide, the Keynesian stability condition can be written  $s(\bar{\pi})\sigma > \beta$ , and the equilibrium solutions for  $u^*$  and  $g^*$  take the form

$$u^* = \frac{\alpha}{s(\bar{\pi})\sigma - \beta} \tag{13}$$

$$g^* = \frac{\alpha s(\bar{\pi})\sigma}{s(\bar{\pi})\sigma - \beta} - \delta \tag{14}$$

#### 2.2 A Harrodian alternative

A Harrodian specification of the investment function makes a distinction between the short-run and the long-run sensitivity of investment to changes in aggregate demand. The insensitivity of investment is plausible in the short run, but changes in aggregate demand have lagged effects on investment, and a weak impact effect (which is required for the stability of the short-run Keynesian equilibrium) does not guarantee that the long-term effects of a sustained increase in aggregate demand and utilization will be weak as well.

In a discrete-time framework (and still assuming, for simplicity, that only utilization matters for investment), the presence of lags can be captured by a general specification,

$$(\frac{I}{K})_{t} = f(u_{t}, u_{t-1}, ..., u_{t-m}, (\frac{I}{K})_{t-1}, (\frac{I}{K})_{t-2}, ..., (\frac{I}{K})_{t-n})$$
(15)

The short-run effect of utilization on accumulation is given by the partial derivative  $\partial f/\partial u_t$ , and the Keynesian stability condition can be written

$$s(\bar{\pi})\sigma > \frac{\partial f}{\partial u_t} \tag{16}$$

The long-run effect of changes in utilization, on the other hand, is given by

$$\hat{K} = \frac{I}{K} - \delta = \phi(u) \tag{17}$$

with

$$\phi'(u) = \frac{d\frac{I}{K}}{du}_{|u_t = u_{t-j}, \frac{I}{K}_t = \frac{I}{K}_{t-k}} = \frac{\sum_{i=0}^{m} \frac{\partial f}{\partial u_{t-i}}}{1 - \sum_{j=1}^{n} \frac{\partial f}{\partial \frac{I}{K}_{t-j}}}$$
(18)

The short-run condition (16) carries no implications for the relation between the long-run sensitivity,  $\phi'$ , and  $s(\pi)\sigma$ . The significance of this point clearly depends on the magnitude of the lagged effects, that is, on the magnitude of the difference between short-run and long-run effects, but there are good reasons to assume, with Harrod, that the difference is large.

The behavioral story behind the Harrodian position is straightforward. For reasons given in the introduction, we are deliberately abstracting from aggregational complications, and firms have a well-defined objective (to maximize profits). Since it would be unreasonable to suppose that demand expectations were persistently and systematically falsified in steady growth, these assumptions make it hard to conceive of a steady-growth scenario in which firms are content to accumulate at a constant rate despite having significantly more (or less) excess capacity than they desire. The only real question concerns the determination of the desired rate of utilization.<sup>6</sup>

The desired utilization rate may deviate from unity. A firm may want to hold excess capacity to deter entry or to enable the firm to respond quickly to variations in demand; or excess capacity may exist simply as a result of indivisibilities of investment (non-convexities in adjustment costs). The desired degree of excess capacity, second, need not be constant over time; changes in the degree of product market competition or in the volatility of demand, for instance, could affect desired utilization rates. Managerial constraints or other bottlenecks, third, may make it difficult or costly to expand capacity at a rapid pace, and the desired utilization rate, consequently, may depend, inter alia, on the rate of accumulation. This case can be represented by equation (17) which specifies a long-run relation between accumulation and desired utilization. In an uncertain environment, fourth, firms may have a range of 'satisfactory' utilization rates, rather than a sharply defined optimal rate, as suggested by Dutt (1990, p. 59). The Harrodian argument, however, does not require the sharp definition. It is sufficient that the satisfactory range be small (a few percentage points); I shall return to this issue in section 3 below.

Simple Harrodian specifications abstract from these complications, the implicit assumption being that the (possibly time-varying) desired utilization rate is independent of the accumulation rate and that the long-run accumulation rate is highly elastic (even if not infinitely elastic) within the relevant range of steady-growth solutions for the rates of accumulation. But whether simple or more elaborate, Harrodian specifications of accu-

<sup>&</sup>lt;sup>6</sup>Chick and Caserta (1997) suggest that although the utilization rate must be at (or near) the desired rate in long-run steady growth, deviations could last for significant periods of time. Long-lasting deviations, however, do not justify a depiction of this medium-run scenario as a self-sustaining equilibrium without internal forces for change.

mulation tend to destabilize the economy: most, but not all, Harrodian inspired models imply that the warranted growth path is locally unstable.

The instability problem has been seen as a powerful argument against a Harrodian approach. The argument may not be spelled out in detail but it is suggested, implicitly, that stability is needed for the model to make sense and/or for the steady-growth path to be empirically relevant (e.g. Lavoie 1995 and Hein et al. 2009). These implicit claims are wrong, I believe. Harrodian models are more complex than the simple Kaleckian model, but they remain tractable and the complexities bring significant rewards (see Skott 2008, Skott and Zipperer 2010). The present paper leaves aside these issues and focuses on the shortcomings of the Kaleckian accumulation function.

#### 3 Theory

A substantial literature discusses the long-run relation between actual and desired utilization rates. Kurz (1986), Committeri (1986). Dumenil and Levy (1993), and Auerbach and Skott (1988) are among those who have faulted Kaleckian models for their failure to ensure that actual utilization and desired utilization coincide in steady growth. One Kaleckian response – adaptive changes in desired utilization – has been articulated in contributions by Lavoie (1995, 1996), Amadeo (1986), Dutt (1997) and Lavoie et al. (2004). I consider this argument first, before turning to the defense based on conflicting targets (Dallery and van Treeck (2008)).<sup>7</sup>

#### Demand induced changes in $u^d$ 3.1

Amadeo, Dutt and Lavoie suggest that the equalization of actual and desired utilization can be reconciled with the long-run variability of the utilization rate if the desired rate of utilization itself becomes an endogenous variable whose rate of change is proportional to the difference between actual and desired utilization.

Mathematically, the argument is set out as follows. Assuming that  $\gamma = 0$ , the investment function (1) can be rewritten

$$\frac{I}{K} = \alpha + \beta u \tag{19}$$

$$= \rho + \beta (u - u^d) \tag{20}$$

$$= \rho + \beta(u - u^d) \tag{20}$$

where  $\rho = (\alpha - \beta u^d)$ . When  $u = u^d$  firms will want to increase their capital stock in line with demand, and the parameter  $\rho$  can be interpreted as the sum of the depreciation

<sup>&</sup>lt;sup>7</sup>The desired rate of utilization is sometimes referred to as the 'normal' rate or the 'target' rate. The terminology itself is not important but may be indicative of underlying differences. Thus, the term 'normal' may suggest something merely conventional, rather than a rate that is determined strategically with reference to well-defined objectives. I shall use the term 'desired utilization rate'; the substantive underlying issues constitute the main topic of this paper.

rate and the expected growth of demand (at the given markup). If  $u^d$  were constant (or more generally, determined independently of actual utilization rates), equation (20) would amount to nothing more than a more complicated version of (1). The Amadeo-Dutt-Lavoie argument, however, suggests that both the expected growth rate of demand and the desired utilization may change endogenously. Specifically, it is assumed that<sup>8</sup>

$$\dot{u}^d = \mu(u - u^d) \tag{21}$$

$$\dot{\rho} = \nu(\frac{I}{K} - \rho) \tag{22}$$

Equation (21) describes the adaptive changes in desired utilization and equation (22) the changes in the expected growth rate. Using (20), equation (22) can be written

$$\dot{\rho} = \nu \beta (u - u^d) \tag{23}$$

The actual utilization rate is equal to

$$u = \frac{\rho - \beta u^d}{s(\bar{\pi})\sigma - \beta} \tag{24}$$

and it follows that the set of stationary solutions to (21)-(22) is given by

$$E = \{ (u^d, \rho) \mid \rho = s(\bar{\pi})\sigma u^d \}$$
 (25)

Starting from any initial position, the economy will converge to a point in this equilibrium set iff the parameters satisfy the stability condition<sup>10</sup>

$$\mu s(\bar{\pi})\sigma > \nu\beta \tag{26}$$

$$\dot{\rho} = \nu(\hat{u} + I/K - \rho)$$

also generates an autonomous two-dimensional system in  $\rho$  and  $u^d$ . The reduced-form expressions for  $\dot{u}^d$ and  $\dot{\rho}$  will be non-linear but the hysteretic properties are retained and a meaningful and stable dynamics imposes qualititatively similar restrictions on the adjustment speeds (stability now requires that  $\nu < \rho + \beta x$ and  $\nu(1 + \frac{\nu(\beta - \mu)}{\beta(\rho - \beta u^d - \nu)}) < \mu \frac{s(\bar{\pi})\sigma}{\beta})$ .

10 Equations (21)-(22) imply that

$$\rho = \frac{\nu \beta}{\mu} u^d + a$$

where, a, the arbitrary constant of integration is determined by initial conditions. Substituting this equation into (24) and the resulting equation for u into (21), we get a one-dimensional differential equation. This equation has a unique stationary solution and it is readily seen that the solution is asymptotically stable iff  $\mu s(\bar{\pi})\sigma > \nu \beta$ .

<sup>&</sup>lt;sup>8</sup>Some writers, including Park (1997) and Commendatore (2006), combine adaptive changes in utilization along the lines of equation (21) with endogenous changes in the markup.

<sup>&</sup>lt;sup>9</sup>The second of these equations does not really capture the adjustment of growth expectations toward actual growth since  $\hat{Y} = \hat{u} + I/K - \delta$ . An alternative specification,

The asymptotic rest point depends on initial conditions and in this sense the model exhibits hysteresis.

From a logical perspective this argument is correct but the authors do not provide much in the way of economic rationale. It may be useful to quote their argument extensively:

• Lavoie 1995 starts by noting that faced with an inconsistency between actual and desired utilization, one possibility is that "firms revise their targeted normal rate of capacity utilization" (p. 805). Having explored the possibilities mathematically, he returns to the economics behind the adjustment by stating that "[f]ollowing a suggestion by Dutt, Amadeo properly described the proposed adjustment mechanism, but without a graphical illustration". This claim is followed by a long quote from Amadeo (1986, p. 155):

"Indeed, one may argue that if the equilibrium degree is systematically different from the planned degree of utilization, entrepreneurs will eventually revise their plans, thus altering the planned degree. If, for instance, the equilibrium degree of utilization is smaller than the planned degree  $(u < u^d)$ , it is possible that entrepreneurs will reduce  $u^d$ ."

• Lavoie et al. 2004, p. 133 suggest that

"Firms hold on to excess capacities to face an uncertain future (Steindl, 1952, p. 2). Firms fear losing customers if they are unable to respond quickly to changes in demand and in the composition of demand. The existence of excess capacity is thus linked to uncertain macroeconomic conditions. The rate of capacity utilization is increased by bringing into use plants that were previously idle. The normal rate of capacity utilization, in that context, is a convention, which may be influenced by historical experience or strategic considerations related to entry deterrence. Although firms may consider the normal rate of capacity utilization as a target, macroeconomic effective demand effects might hinder firms from achieving this target, unless the normal rate is itself a moving target influenced by its past values."

• Dutt 1997 provides a little more detail. Replacing his notation with the one in this paper  $(u^d, \rho, \beta)$  instead of  $u_n, x, \lambda$ , Dutt presents the following argument (pp. 246-247):

"Explanations for this equation can be developed depending on what one takes to be the determinant of  $u^d$  at any point in time. If it is taken to be determined simply by the actual experience of firms, if actual utilization exceeds (is less than) what firms previously considered normal, they will adjust what they consider normal upwards (downwards). Alternatively, if it is taken to be determined be strategic considerations, so that firms may reduce their normal

(or desired) capacity utilization if they expect a higher rate of entry than at present, and we take entry to be proportional to investment rates, then we obtain an equation such as

$$du^d/dt = -\mu'(\rho - \frac{I}{K})$$

This equation, using (17) [the investment function (20) in this paper, PS] and the short-run equilibrium condition implies equation (23) [equation (21) in this paper, PS] where  $\mu = -\mu'\beta$ ."

The argument in Lavoie (1995) and Amadeo (1986), first, does not go beyond stating the formal possibility of an adjustment. Amadeo may seem to provide an argument, and it is hard to take issue with his statement that "if the equilibrium degree is systematically different from the planned degree of utilization, entrepreneurs will eventually revise their plans". But why not adjust the rate of accumulation - the Harrodian argument - rather than the target? Adjustments in the target would only be justified if the experience of low actual utilization makes firms decide that low utilization has now become optimal, and neither Amadeo nor Lavoie presents an argument for this causal link.

Lavoie et al. (2004) suggest that in the presence of uncertainty, the desired degree of utilization must be conventional, and since conventions are rooted in history, the adaptive formulation therefore seems appropriate. One can only agree that uncertainty is a fact of life and that firms cannot maximize profits in a strict and rigorous sense of the word. In their pursuit of profit firms follow routines and have perceived constraints that contain a conventional element. But the presence of uncertainty and conventional elements does not mean that the desired utilization rate is a purely conventional variable. Consider a simple example. I may not know exactly how long it will take me to get to work in the morning since weather, traffic and many other variables may influence the commuting time. Still, uncertainty of this kind and the fact that I may not have a rigorously derived optimal departure time do not imply that my desired arrival time adjusts adaptively toward the actual arrival time. Imagine that over a period I am late for class every day because of a series of minor mishaps (a flat tire one day, followed by a snow storm the next day, road works, a traffic accident at a key intersection, ...). I do not respond to this unfortunate string of events by adjusting my planned arrival time in the way suggested by Lavoie: I may have been late for class (have had too little actual 'commuting capacity') because of unforeseen shocks but that does not make being late seem desirable. In this example, nothing prevents me from adjusting my departure time in the direction that I consider optimal, and in this respect there might seem to be a difference compared with firms' investment decisions: if all firms try to increase their utilization rates by reducing investment, the macroeconomic impact is a decline in aggregate demand which aggravates the original problem.

Lavoie et al. use the instability problem as a second argument (the last sentence in the above quotation). They imply that the endogenous adjustment of target to realized value is necessary if any reconciliation between the two is to be achieved. This there-is-noalternative argument is unwarranted as many other mechanisms can produce a long-run
consistency between average and desired utilization (Skott (2010) takes up this issue).
Moreover, even if this were not the case, a purely functional argument carries little weight.
The stability argument for adaptation presumes that individual firms (i) are aware of
the demand externalities associated with their investment decisions, (ii) act upon this
insight, even if it goes against their narrow self-interest, and (iii) with this insight and
the willingness to act on it, choose to adjust their planned utilization rate to the actual,
rather than adjust their actual accumulation rate so as to generate a level of aggregate
demand that will adjust their actual utilization rate to their desired rate. These behavioral
assumptions seem peculiar.

Disregarding his pure inertia possibility, Dutt (1997) suggests that firms reduce their desired rate of utilization if the threat of entry goes up. This argument suggests that the desired utilization rate is related to the level of the threat of entry, and the latter variable is assumed "to be proportional to investment rates". The argument therefore yields a relation between  $u^d$  and I/K. A relationship of this kind between the level of desired utilization and an indicator of the need for deterrence is plausible and quite standard in the literature, although the sensitivity of  $u^d$  to variations in the threat of entry is likely to be low and one may question the use of I/K as the main indicator of the need for deterrence.<sup>11</sup>

The formal equation, however, does not specify a relation between  $u^d$  and I/K. A level equation of this kind would generate a dynamic system consisting of a single differential equation in  $\rho$  (with an unstable stationary solution), and there would be neither adaptation nor hysteresis. Instead, Dutt's equation relates the change in desired utilization to the difference between the expected growth of demand and the actual rate of accumulation. No argument is provided for this specification, and it is not obvious how deterrence can justify the equation. Why, for instance, is the desired degree of excess capacity increasing – without bounds – whenever the expected growth of demand exceeds the rate of accumulation?

Habits and conventions undoubtedly play a role in firms' perceptions of the optimal degree of excess capacity, and it would be churlish to deny any adaptive influence of actual on desired utilization. The Amadeo-Dutt-Lavoie formulation, however, requires not just the existence of some element of adaptation but the presence of adaptation that is both quantitatively fast and unbounded. The unboundedness is embedded in the functional form (21), which implies that if utilization were to remain at, say, fifty percent then firms would eventually come to view fifty percent as the desired utilization rate; the need for fast adjustment in  $u^d$  (relative to the adjustment speed for expected demand growth) is

 $<sup>^{11}</sup>$ An increase in the profit share, for instance, makes entry more attractive and gives existing fims an increased incentive to create extra capacity as a deterrence. But again, the effect on  $u^d$  is likely to be modest. Certainly, it would be hard to explain why firms should want to reduce their utilization to such an extent that the profit rate (evaluated at desired utilization) declines as a result of the increase in the profit share. Yet, this is the implication of the Kaleckian 'paradox of cost'.

an implication of the stability condition (26). These assumptions do not seem reasonable, and the specification cannot be seen as just a local approximation that is acceptable within a relevant range of 'satisfactory' utilization rates. There is no empirical evidence to support the assumption of fast adjustments in  $u^d$  and as argued in section 4 below, the theory needs a range of potential  $u^d$ -values that is much larger than any plausible range of demand-induced variations.

Adaptive behavior is used widely in economic models and often makes good sense. Adaptive inflation expectations, for instance, perform well for most advanced countries in most of the second half of the 20th century (but not necessarily for other periods and countries), and one can tell a persuasive story: the adaptive mechanism concerns a variable - inflation - which is outside the control of the individuals forming the expectation and which in this period had neither a clear long-term trend nor obvious tendencies to revert to some well-defined fundamental value. As another example, adaptive changes have been used to explain employment hysteresis. In insider-outsider models the story is straightforward: the set of insiders itself may change adaptively as a result of shocks to employment, and these changes naturally feed into wage demands and employment (Blanchard and Summers 1987). Alternatively, wage aspirations (fairness norms with respect to wages) may change adaptively. Workers who have grown accustomed to three percent real-wage increases during a period with high productivity growth may only gradually adjust their aspirations if real-wage increases drop to one percent a year, and adaptive changes in aspirations may generate employment hysteresis (Skott 1999, 2005). As in the inflation example, the adaptive process relates to a variable - real wage increases - that cannot be controlled by the workers who form the aspirations: workers may demand a particular increase in money wages but have no control over inflation; they have no direct way of getting reliable evidence on the prospects of their own firm; they cannot know the future overall pace of technical progress or even gauge its recent pace accurately, and they have no way of knowing whether the range of feasible real wage increases have changed.

A firm's utilization rate is a very different category. A firm controls its own investment and is under no obligation to keep investing if it finds itself with unwanted excess capacity. Nor is there any reason why a negative demand shock and a decline in sales should make the firm think that the optimal degree of excess capacity has changed permanently. Indeed, the asymmetry in the treatment of labor and capital in the Kaleckian model is striking in this respect. It is usually assumed that the desired output-labor ratio is simply equal to the maximum determined by the fixed coefficient production function and that this maximum is continuously maintained. In reality, adjustment of the labor input is neither costless nor instantaneous, and firms may want to engage in labor hoarding, at least temporarily. Moreover, labor hoarding may be explained partly by the same arguments that account for excess capital capacity (fluctuating demand, for instance, and

<sup>&</sup>lt;sup>12</sup>The availability of financing and other external constraints may come into play for a firm that wants to expand capacity but are irrelevant for the stripped-down model and have not been invoked in defence of the basic Kaleckian specification.

the difficulties and costs of finding skilled labor quickly in case of increasing demand). Yet, no Kaleckian model (to my knowledge) has made a case for adaptive changes in the optimal degree of labor hoarding. The optimal rate of labor utilization is taken to be exogenously given and for simplicity is set equal to one (whether it is one or some other constant makes no substantive difference). This simplifying assumption about the demand for labor is perfectly reasonable but the implicit motivation for the assumption - profit maximizing behavior and a well-defined desired rate of labor utilization - suggests that capital utilization be treated in a similar way. Profit maximizing firms do not keep workers that they do not need; why would they want to maintain undesired excess capacity?

#### 3.2 Competing targets

A recent contribution by Dallery and van Treeck (2008) suggests that a firm may indeed want to accept permanent deviations from desired utilization.<sup>13</sup> The crux of their argument is that "in situations of conflict within the firm it may simply be impossible for firms to realise both their utilisation and their profitability target" (p.7) and that the deviation of u from  $u^d$  (or  $u^t$  in their notation) enables the firm to realize the more important profitability targets.

Dallery and van Treeck identify two sets of conflict: one between managers and share-holders over the objectives of the firm (growth or profit maximization) and one between management and workers over the share of wages (the size of the markup).

The first conflict leads to the formulation of the firm's profitability target as a weighted average of the targets of managers and shareholders. Different regimes, it is suggested, may correspond to different weights and in some but not all regimes, the profitability target may change endogenously. These complications and extensions are irrelevant for present purposes, and we may take the (conflict determined) target rate of profit as given.

The conflict over wages is modeled in terms of two equations, one for price inflation (which is influenced by the profit target) and one for wage inflation (which is influenced by workers' wage target). The two inflation rates must be equal in steady growth, and this condition determines the value of the markup and the profit share.<sup>14</sup> The model is completed by postulating a saving function and a Kaleckian investment function (other variables, aside from utilization, are also included in the investment function but these are irrelevant for present purposes).

Not surprisingly, the equilibrium solution of this model shows a discrepancy between actual and desired utilization. Conflict enters as a way of endogenizing the markup, but the rest of the story amounts to a simple Kaleckian specification.

Dallery and van Treeck see it differently. They suggest that

<sup>&</sup>lt;sup>13</sup>This defense of the Kaleckian position, which builds on suggestions by Lavoie (2003), is also given prominence in Hein et al.'s (2008) survey of instability puzzles in Kaleckian models.

<sup>&</sup>lt;sup>14</sup> Algebraically, the solution for  $r_s$  in Dallery and van Treeck's equation (8) is substituted into their equation (4). Since, by assumption,  $u_s$  is exogenous, we now have a solution for the markup.

"As soon as workers have some power to oppose firms' "distribution objective" ... firms have to operate above standard utilisation ... in order to reach their profitability objectives ..... We arrive at a "fully-adjusted position" regarding profitability, but this does not coincide with a fully-adjusted position in the usual sense. The rate of utilisation is still seen as a free variable, and this ensures that firms' and workers' objectives are not fully contradictory, as variations in utilisation allow them to partly reconcile their respective profitability and distribution targets"

(p. 13; italics in original; the omitted parts give algebraic statements of the differences between targets and realizations)

The core of this statement is the observation that if firms have a target for the profit rate and workers a target for the wage share then these targets can be made mutually consistent if the utilization rate is a free variable. This is clearly correct but does not establish that utilization will be a free variable.

The Dallery and van Treeck argument does not address the key issue: does the specification of the investment function give a plausible representation of firm behavior? Putting it differently, they claim that important conflicts within the firm (that is, within the individual firm) lead to the firm's acceptance of utilization rates that deviate from the desired level, even in the long run. But they do not substantiate this claim: they fail to show what internal conflicts prevent a firm from trying to adjust its utilization rate toward what it considers optimal.

Consider a firm that finds itself with much more capacity than the managers would like. Why would shareholders and / or workers insist that the firm keep accumulating capital at a constant rate if the firm does not need capital and the new machines will be idle? What conflicts or actions on the part of other stakeholders prevent the firm from scaling down its investment plans in order to reduce the degree of excess capacity? Dallery and van Treeck do not consider these questions. They derive some macroeconomic implications of a model that assumes a standard Kaleckian specification of the investment function.

#### 4 Evidence

#### 4.1 Stylized facts

Stable versions of the adaptive model based on (21)-(22) imply that the long-run outcomes can be described using equations that are qualitatively identical to the ones for the simple

Kaleckian model. In steady growth, we have

$$u = u^d (27)$$

$$g = \rho \tag{28}$$

$$g = \rho \tag{28}$$

$$s(\bar{\pi})\sigma u = \frac{S}{K}$$

$$\frac{I}{K} = a + \frac{\beta \nu}{\mu} u = a + bu \tag{30}$$

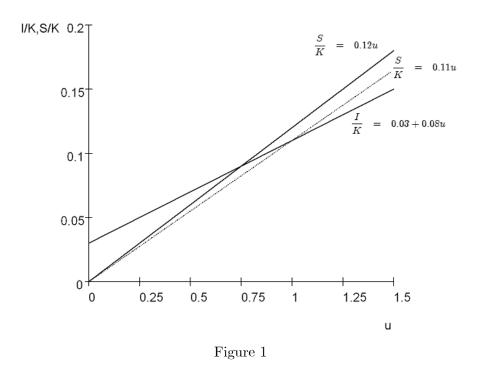
Equations (27)-(28) describe the stationarity conditions for (21)-(22) and equation (29) is the saving function. Equation (30) follows from (20)-(22) upon integration (see footnote

The model is illustrated graphically in Figure 1. Unlike most illustrations, which focus on the qualitative properties, figure 1 is based on Kaleckian benchmark values. Empirically, the gross saving rate  $s(\pi)$  typically falls in the range 0.15-0.3 and the technical capital-output ratio in the range 1-3. Figure 1 uses  $s(\pi)\sigma = 0.12, b = 0.08$  and a = 0.03, yielding an equilibrium utilization rate of  $u^* = a/(s(\bar{\pi})\sigma - b) = 0.75$ .

Figure 1 and the numerical example illustrate one of the main weaknesses of the Kaleckian analysis. Assume that the saving rate drops slightly, with  $s(\bar{\pi})\sigma$  falling from 0.12 to 0.11. As a result, the growth rate increases by 2 percentage points while the utilization rate jumps from 75% to 100%. This strong sensitivity of utilization to variations in parameters is an intrinsic property of the Kaleckian model. For any reasonable specification of the saving function, the Kaleckian stability condition puts a very low ceiling on the maximum value of b (about 0.1). Shocks to the saving function therefore give rise to fluctuations in utilization rates that are at least about ten times larger than those in accumulation. Shocks to the accumulation function (changes in a) produce movements along the saving function and (given the stability condition) the ratio of variations in utilization to variations in the growth rate is slightly larger, but still unlikely to be much below ten. These implications do not fit the data.<sup>15</sup>

<sup>&</sup>lt;sup>15</sup>The existence of non-linearities in the saving function might seem to offer a solution. A sigmoid shaped saving function could make saving sensitive to variations in utilization in a relevant range of utilization rates and also produce average saving rates that are in line with observations. A non-linearity of this kind would allow the investment function to be steeper too (in the relevant range), while still preserving the stability condition. Unfortunately, I am aware of neither theoretical arguments nor empirical evidence to support this type of non-linearity of the long-run saving function.

Non-linearities have sometimes been suggested in the literature. Kaldor's (1940) model of a trade cycle. for instance, has a non-linearity. The plausibility of the specification for the long run may be questionable, but the non-linearity is also of the opposite kind: Kaldor takes the saving function to be relatively flat for an intermediate range of output.

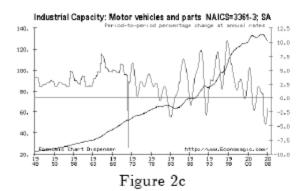


Figures 2a-2j show the movements in total capacity and in the rate of capacity utilization for US manufacturing as a whole as well as for some individual industries that have experienced turbulent demand conditions and therefore may be of particular interest. Capacity utilization exhibits significant short-run variation - as one would expect - but the long-run variation is modest. Thus, the stylized facts on utilization and growth do not appear to have the characteristics implied by the Kaleckian assumptions. In order for the Kaleckian model to generate long-run variations in u that are of the same order of magnitude or smaller than those in accumulation, one would need a strong positive correlation between the shocks to investment and to saving (or at the industry level, a strong correlation between shocks to the industry specific investment function and shocks to industry demand). To my knowledge no reasons have been offered for this kind of positive correlation between the shocks (and from a Keynesian/Kaleckian perspective, moreover, it would seem strange to suggest that shocks to saving will always be accompanied by shocks to investment that go in the same direction).

The measurement of productive capacity raises both conceptual and practical problems and one may question the data on utilization. (Shapiro 1989). The Federal Reserve data for the US are based on a combination of different surveys and other information, and the Fed adjusts its measure of capacity in various ways to get a measure that it considers reasonable. The data problems are both real and serious but one would need a strong argument to believe that biases in measured utilization explain the discrepancy between Kaleckian predictions and stylized facts.



Figure 2a



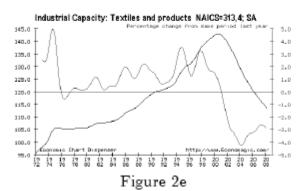
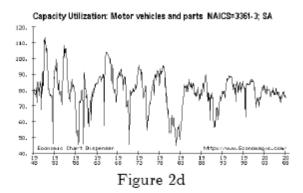
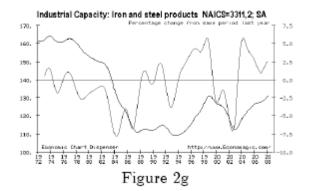




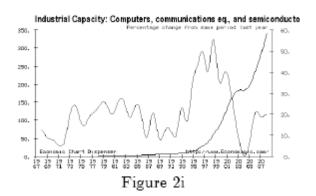
Figure 2b

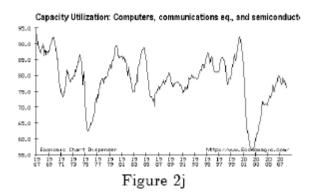












#### 4.2 Econometric evidence

Investment functions are notoriously ill-behaved and the econometric evidence is mixed and relatively weak. Moreover, the implications of econometric results for the Kaleckian position can be unclear since some variables in the estimated equations may be influenced by or strongly correlated with the utilization rate, which itself does not even appear in many econometric specifications.<sup>16</sup>

A careful and detailed examination of the econometric literature and its implications

$$\Delta \log I = -0.59 + 1.59 \Delta \log Y + 0.84 \Delta \log Y - 1 + 0.38 \Delta \log R - 0.18 \Delta \log R_{-1} - 0.21 \log \frac{I_{-1}}{Y_{-1}} + 0.03 \log R_{-1} + 0.00 \log R_{-1} + 0.00$$

where R is profits. The appearance of  $\log R_{-1}$  seems peculiar, given that all other variables are in growth rates or expressed as ratios (and in fact the coefficient on  $\log R_{-1}$  is statistically insignificant). Disregarding this problem, Stockhammer et al see this equation as part of - and consistent with - a Kaleckian model. In steady growth, however,  $\Delta \log I = \Delta \log Y = \Delta \log Y_{-1} = \Delta \log R = \Delta \log R_{-1} = g$ , and we get a long-run relation

$$1.63g = 0.59 + 0.21 \log \frac{I_{-1}}{Y_{-1}} - 0.03 \log R_{-1}$$

 $<sup>^{16}</sup>$ Stockhammer et al. (2007), for instance, estimate the following investment function on data for the Euro-area:

for the Kaleckian model is beyond the scope of the present paper and will be left for future research. A recent paper by Lavoie et al. (2004), however, sets out to test the Kaleckian specification against some competing specifications.

Having acknowledged that a number of variables - including financial variables - have been found to influence investment, Lavoie et al. note that "the crucial distinctive features of the post-Keynesian and Marxist investment models ... are located in the role of the rate of capacity utilization" (p.129). Using Canadian data, they proceed to estimate stripped-down versions of four different specifications, two "Marxist" specifications, a "naive Kaleckian" version (equation (1) with  $\gamma=0$ ), and a sophisticated "hysteresis-Kaleckian" version (based on equations (20)-(22) above). In the conclusion (p. 146) they summarize their results as follows:

"our regression results show that the (HK) equation [the "hysteresis Kaleckian" specification; PS] performs better than the other three specifications stipulated above, using standard indicators such as  $R^2$ , F-statistics, and t-ratios. It also performed better when various comparative diagnostic tests, information criteria, and encompassing tests were applied, whatever the precise test being applied. These statistical tests allow us to conclude that the sophisticated Kaleckian investment function (HK) is the preferred investment function."

There are two problems with this conclusion. The estimated empirical HK equation, first, bears no relation to the theoretical model. In order to derive a discrete-time, empirical version of the HK investment function, Lavoie et al. subtract an equation for  $(I/K)_{t-1}$  from the equation for  $(I/K)_t$  to get

$$\frac{I_t}{K_t} - \frac{I_{t-1}}{K_{t-1}} = \rho_t - \rho_{t-1} - \beta(u_t^d - u_{t-1}^d) + \beta(u_t - u_{t-1})$$

$$= \nu(\frac{I_{t-1}}{K_{t-1}} - \rho_{t-1}) - \beta\mu(u_{t-1} - u_{t-1}^d) + \beta(u_t - u_{t-1}) \tag{31}$$

Since  $\frac{I}{Y} = \frac{I}{K} / \frac{Y}{K} = (g + \delta) / (u\sigma)$  and leaving out the insignificant and hard-to-interpret term  $\log R_{-1}$ , we can rewrite this equation as

$$1.63g - 0.21\log(g + \delta) = 0.59 - 0.21\log u - 0.21\log \sigma$$

The implied long-run effect of changes in utilization on accumulation can now be found. Assuming a constant technical coefficient,  $\sigma$ , and taking total derivatives we get

$$(1.63 - \frac{0.21}{q+\delta})dg = -.21\frac{du}{u}$$

and hence

$$\frac{dg}{du} = \frac{0.21}{\frac{0.21}{g+\delta} - 1.63} = \frac{g+\delta}{1 - 7.76(g+\delta)}$$

The expression on the right hand side is negative if  $g + \delta > 0.13$  and increasing in  $g + \delta$  when  $g + \delta < 0.13$  with an asymptote at  $g + \delta = 0.13$ . To get a plausible Kaleckian value for the long-run sensitivity of accumulation to utilization - a value in the range between zero and 0.15 - the value of  $g + \delta$  would have to be less than 0.07.

where the second equality uses a discrete-time version of (21)-(22). Noting, then, that the variables  $\rho$  and  $u^d$  are unobservable they proceed as follows:

"in the sophisticated Kaleckian view, the rate of utilization, which is considered to be normal, is influenced by its past values. ... For our purposes, we shall use an established, simple and direct approach for the two Kaleckian equations that consists of applying the HP filter ... to  $u_t$ . This procedure allows us to identify an estimate of the permanent component in the series  $u_t$ , which we denote as the series  $u_n$  [corresponding to  $u^d$ ; PS]."

A Hodrick-Prescott filter does not capture the adaptive formulation in (20)-(22). It simply smooths the time series, attaching as much weight to future observations as to past. Figure 3 shows the actual and filtered series for utilization, using Lavoie et al.'s Canadian data for the manufacturing sector. The filtered series clearly does not increase whenever actual utilization exceeds the smoothed value and fall whenever actual utilization is below. As one would expect, a regression of the change in the smoothed series on the difference between to two series gives a parameter estimate that is statistically insignificant.

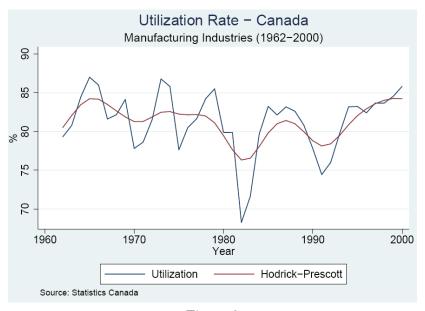


Figure 3

Although the Hodrick-Prescott filter does not capture the hysteresis argument, a smoothed version of actual utilization rates could be a useful approximation for a structurally determined, desired utilization rate: as argued above, the desired utilization rate may be time-varying and if the actual rate fluctuates around the desired rate, the Hodrick-Prescott filter may provide a good estimate. Thus, paradoxically, while the empirical HK equation is inconsistent with the adaptive model, this type of equation could represent

an empirical version of the Harrodian argument. The interpretation of the coefficients in the estimated equation, however, is unclear because of the inclusion of both  $I/K-\rho$  and  $u-u^d$  as explanatory variables (if, in fact, (20)-(22) had held, the two variables would have been proportional, except perhaps for a stochastic disturbance term). Table 1 presents the results of OLS regressions that leave out the  $I/K-\rho$  term (using the same Canadian data for manufacturing as Lavoie et al.). Column 3 leaves out the change in utilization rates as an explanatory variable; columns 1 and 2 follow Lavoie et al. and retain this variable. The Harrodian rationale for this would be that changes in accumulation take into account not just the discrepancy between actual and desired utilization but also whether current accumulation rates are already generating changes in the right direction. It is unclear whether, from this perspective, the change in utilization should be lagged, and columns 1 and 2 differ in this respect. Column 1 clearly outperforms the other two specifications but all three specifications give the expected positive coefficient on  $u-u^{HP}$ , and in columns 1 and 3 the coefficient is significant at the 1 percent level. 17

"HK" Equation Estimation Dependent variable:  $\Delta g_{k,t} = \Delta(\log K_t - \log K_{t-1})$ 

	(1)	(2)	(3)
$u_{t-1} - u_{t-1}^{HP}$	0.3400*** [0.0499]	0.0757 [0.0624]	0.1753*** [0.0529]
$\Delta u_t$ $\Delta u_{t-1}$	0.1961*** [0.0353]	0.1177**	
Constant	-0.1341	[0.0442] -0.1252	-0.1164
Observations	$\frac{[0.1049]}{39}$	$\frac{[0.1306]}{39}$	$\frac{[0.1374]}{40}$
$R^2$	0.58	0.35	0.22

Standard errors in brackets \*\*\* p<0.01, \*\* p<0.05, \* p<0.1

Table 1

<sup>&</sup>lt;sup>17</sup>Hein and Schoder (2009) estimate investment functions for Germany and the US. Like Lavoie et al., they regress the change in accumulation on deviations of actual utilization from an HP-trend. Their statement of the long run implications (Table 3) is incorrect, however, and their results in Table 2 support a Harrodian view with a long-run accumulation rate that is perfectly elastic.

Returning to the "hysteresis equation" (31), there is a standard procedure for dealing with the unobservability of  $\rho$  and  $u^d$ : Koyck transformations. Note first that using (21)-(22) we have

$$\rho_t - \rho_{t-1} = \frac{\nu \beta}{\mu} (u_t^d - u_{t-1}^d) \tag{32}$$

and hence

$$\rho_t = \frac{\nu \beta}{\mu} u_t^d + A \tag{33}$$

where A is an arbitrary constant.<sup>18</sup> Using (20)-(22) and (33), the accumulation function can now be written

$$\frac{I_t}{K_t} = A + \beta (\frac{\nu}{\mu} - 1) u_t^d + \beta u_t 
= A + \beta (\frac{\nu}{\mu} - 1) [\mu u_{t-1} + (1 - \mu) u_{t-1}^d] + \beta u_t$$
(34)

Subtracting  $(1 - \mu) \frac{I_{t-1}}{K_{t-1}}$  from both sides we get

$$\frac{I_t}{K_t} - (1 - \mu) \frac{I_{t-1}}{K_{t-1}} = \mu A + \beta (\nu - 1) u_{t-1} + \beta u_t$$
(35)

or

$$\frac{I_t}{K_t} - \frac{I_{t-1}}{K_{t-1}} = \mu A - \mu \frac{I_{t-1}}{K_{t-1}} + \beta \nu u_{t-1} + \beta (u_t - u_{t-1})$$
(36)

This estimation contains no unobservable variables and, using the same Canadian data as Lavoie et al., a standard OLS regression yields the results in Table 2. The implied estimates of the parameters are  $\beta=0.11,\,\mu=0.11,\,\nu=1.40.$  Thus, the stability condition -  $\frac{\beta\nu}{\mu} < s(\bar{\pi})\sigma \approx 0.1$  - is not even close to being satisfied.<sup>19</sup>

To avoid misunderstanding, the econometric results in this section are highly preliminary and clearly do not settle the issue. They do show that some of the claims that have been made in favor of Kaleckian specifications are unfounded, but much more work needs to be done.

 $<sup>^{18}</sup>$ If one or both of the equations (21) and (22) include an additive stochastic term, the constant A will itself become a stochastic variable, and if the disturbance terms are iid, A would be a random walk. I shall take A to be a constant.

<sup>&</sup>lt;sup>19</sup>Skott and Zipperer (2009) reach a similar conclusion. Using monthly US data, they find a long-run effect of utilization on accumulation of about  $\partial \frac{I}{K}/\partial u = 1$ .

Corrected H	K Equation		
Dependent variable: $\Delta g_{k,t}$ )			
$g_{k,t-1}$	-0.1118		
	[0.0838]		
$u_{t-1}$	0.1577***		
	[0.0372]		
$\Delta u_t$	0.1133**		
	[0.0416]		
Constant	-12.6283***		
	[3.0234]		
Observations	39		
$R^2$	0.38		
3.7 · · · · · · · · · · · · · · · · · · ·			

Notes: Standard errors in brackets. \*\*\* p<0.01, \*\* p<0.05.

Table 2

#### 5 Conclusion

The canonical Kaleckian model largely ignores or assumes away stability issues. It is not controversial to assume that a short-run investment function (where all the effects of lagged variables can be thought of as being part of the constant) will satisfy a Keynesian stability condition, but the Kaleckian model leaves out lags and assumes that the short-run specification applies in the long run as well. This elimination of lags and dynamics simplifies the analytics enormously, with obvious pedagogical benefits, and the static equations of the Kaleckian model provide a flexible platform for extensions in many directions. The specification of the accumulation function, however, is critical for the properties of the model, and at a methodological level the basic model sends the wrong message if in fact lags, dynamics and instabilities are essential for an understanding of capitalist economies.

The significance of these concerns clearly hinges on whether there is theoretical and empirical evidence to support the Kaleckian specification. If there is, then the simplicity of the framework is a strength rather than a weakness. This paper suggests that the evidence is weak, both on the theoretical and empirical side.

The empirical analysis in section 4 is sketchy and incomplete. There are significant data issues, the estimation of investment functions is notoriously difficult, and a much

more careful analysis is needed to allow decisive conclusions. Still, the evidence, such as it is, fails to support the Kaleckian position.

The theoretical argument, it seems to me, is clearer. Most contributors accept that a steady-growth path should be characterized by a consistency between actual and desired utilization rates, and if the economy tends to fluctuate around a steady growth path, this steady-growth property implies that average utilization rates will be close to the desired rate.<sup>20</sup> The real question concerns the determination of the desired rate.

Mathematically it is not difficult to set up a model that generates Kaleckian results. The desired rate may adapt to the actual rate, and assuming certain conditions with respect to adjustment speeds, we may get a model that generalizes the canonical model; the key properties of the simple model are retained but, because of the non-uniqueness of the stationary solution, the possibility of hysteresis effects are present. The behavioral story behind the equations does not, however, seem plausible.

"Plausibility" is a matter of judgement and there are no hard and universal rules. Most of contemporary economics remains committed to an optimization paradigm which requires that all equations be derived from some strict optimization problem. This requirement, often misleadingly sold as "microfoundations", glosses over aggregational issues, imposes unreasonable powers of foresight and cognition on all economic actors, and tops it all by then analyzing only grossly simplified decision problems since more complex problems defy solution. These shortcomings of mainstream methodology do not, however, imply that macroeconomic equations should be posited without consideration of how they relate to the behavior of firms and households, taking into account as best one can both the diversity of behaviors and the influence of institutional structures. In fact, Keynes along with some of the old Keynesians seem to have it just about right in this respect (see, for example, Tobin 1986). Macroeconomists need to tell a convincing behavioral story, drawing on whatever evidence seems relevant, and to my mind the Kaleckians have yet to do that with respect to investment.

#### References

- [1] Amadeo, E. (1986) "The role of capacity utilization in long-period analysis". *Political Economy*, 2 (2), pp. 147-185.
- [2] Auerbach, P. and Skott, P. (1988) "Concentration, competition and distribution." International Review of Applied Economics, 2, pp. 42-61.
- [3] Blanchard, O. and Summers, (1987) "Hysteresis in Unemployment." European Economic Review, 31, 1/2, pp. 288-295.

<sup>&</sup>lt;sup>20</sup>There may be some deviation between the two since in general the time-average of a variable that fluctuates around some stationary equilibrium need not be equal to the stationary value.

- [4] Blecker, R. (1989) "International competition, income distribution and economic growth". Cambridge Journal of Economics, 14, pp. 375-393.
- [5] Blecker, R. (1999) "Kaleckian Macro Models for Open Economies." In J. Deprez and J.T. Harvey (eds) Foundations of International Economics: Post Keynesian Perspectives. London: Routledge.
- [6] Caballero, (1999) "Aggregate Investment." In J. B. Taylor and M. Woodford (eds.), Handbook of Macroeconomics. Amsterdam: Elsevier.
- [7] Chick, V. and Caserta, M. (1997) "Provisional equilibrium in macroeconomic theory". In P. Arestis, G. Palma and M. Sawyer (eds) Capital Controversy, Post-Keynesian Economics and the History of Economic Thought: Essays in Honour of Geoff Harcourt, Vol. II. London: Routledge.
- [8] Commendatore, P. (2006) "Are Kaleckian models relevant for the long run?" In N. Salvadori and C. Panico (eds) Classical, Neoclassical and Keynesian Views on Growth and Distribution, Cheltenham: Elgar.
- [9] Committeri, M. (1986) "Some comments on recent contributions on capital accumulation, income distribution and capacity utilization. *Political Economy*, 2, pp. 161-186.
- [10] Dallery, T. and van Treeck, T. (2008) "Conflicting claims and equilibrium adjustment processes in a stock-flow consistent model". IMK Working Paper 09/2008. Forthcoming in *Review of Political Economy*.
- [11] Dos Santos, C.H. and Zezza, G. (2008) "A simplified, 'benchmark', stock-flow consistent Post-Keynesian growth model". *Metroeconomica*, 59 (3), pp. 441-478.
- [12] Dumenil, G. and Levy, D. (1993) The economics of the profit rate. Aldershot: Elgar.
- [13] Dutt, A.K. (1984) "Stagnation, income distribution and monopoly power". Cambridge Journal of Economics, 8, pp. 25-40.
- [14] Dutt, A.K. (1990) Growth, Distribution and Uneven Development. Cambridge: Cambridge University Press.
- [15] Dutt, A.K. (1997) "Equilibrium, path dependence and hysteresis in post-Keynesian models". In P. Arestis, G. Palma and M. Sawyer (eds) Capital Controversy, Post-Keynesian Economics and the History of Economic Thought: Essays in Honour of Geoff Harcourt, London: Routledge.
- [16] Flaschel, P. and Skott, P. (2006) "Steindlian models of growth and stagnation." *Metroeconomica*, 57 (3), pp. 303-338.

- [17] Hein, E. and van Treeck, T. (2007) "'Financialisation' in Kaleckian/Post-Kaleckian models of distribution and growth". IMK Working Paper 7/2007.
- [18] Hein, E., Lavoie, M. and van Treeck, T. (2008) "Some instability puzzles in Kaleckian models of growth and distribution: a critical survey". IMK Working Paper 19/2008...
- [19] Kaldor, N. (1940). "A model of the trade cycle". Economic Journal, 50, pp. 78-92
- [20] Kurz, H. (1986) "Normal positions and capital utilization." Political Economy, 2 (1), pp. 37-54.
- [21] Lavoie, M. (1995) "The Kaleckian model of growth and distribution and its neo-Ricardian and neo-Marxian critiques." Cambridge Journal of Economics, 19, pp. 789-818.
- [22] Lavoie, M. (1996) "Traverse, hysteresis, and normal rates of capacity utilization in Kaleckian models of growth and distribution". Review of Radical Political Economics, 28 (4), pp. 113-147.
- [23] Lavoie, M. (2003). "Kaleckian effective demand and Sraffian normal prices: towards a reconciliation". Review of Political Economy, 15, pp. 53-74.
- [24] Lavoie, M. and Godley, W. (2001-2002) "Kaleckian models of growth in a coherent stock-flow monetary framework: a Kaldorian view." Journal of Post Keynesian Economics, 24 (2), pp. 277-311.
- [25] Lavoie, M., Rodriquez, G. and Seccareccia, M. (2004) "Similarities and Discrepancies in Post-Keynesian and Marxist Theories of Investment: A Theoretical and Empirical Investigation". *International Review of Applied Economics*, 18 (2), pp. 127-149.
- [26] Lima, G.T. and Setterfield, M. (2008) "Inflation Targeting and Macroeconomic Stability in a Post Keynesian Economy". *Journal of Post Keynesian Economics*, forthcoming.
- [27] Marglin, S. and Bhaduri, A. (1990) "Profit Squeeze and Keynesian Theory." In: S. Marglin and J. Schor (eds). The Golden Age of Capitalism - Reinterpreting the Postwar Experience. Oxford: Clarendon.
- [28] Park, M.-S. (1997) "Accumulation, capacity utilisation and distribution". Contributions to Political Economy, 16, pp. 87-101.
- [29] Robinson, J. (1962) Essays in the theory of economic growth. London and Basingstoke: Macmillan.
- [30] Rowthorn, B. (1981) "Demand, real wages and economic growth." *Thames Papers in Political Economy.*

- [31] Shapiro, M.D. (1989) "Assessing the Federal Reserve's Measures of Capacity and Utilization". *Brookings Papers on Economic Activity*, 1:1989, pp. 181-225.
- [32] Skott, P. (1989) Conflict and Effective Demand in Economic Growth. Cambridge: Cambridge University Press.
- [33] Skott, P. (1999) "Wage Formation and the (non-) existence of the NAIRU". *Economic Issues*, March, pp. 77-92.
- [34] Skott, P. (2005) "Fairness as a Source of Hysteresis in Employment and Relative Wages". *Journal of Economic Behavior and Organization*, Vol. 57, 2005, pp. 305-331.
- [35] Skott, P. (2010) "Growth, instability and cycles: Harrodian and Kaleckian models of accumulation and income distribution". Working Paper 2008-12, Department of Economics, University of Massachusetts Amherst. Forthcoming in M. Setterfield (ed.) Handbook of Alternative Theories of Economic Growth, Elgar.
- [36] Skott, P. and Zipperer, B. (2009) "Dynamic patterns of accumulation and distribution". Mimeo. Forthcoming (in Japanese) in *Kikan Keizai Riron*.
- [37] Steedman, I. (1992) "Questions for Kaleckians". Review of Political Economy, 4 (2), pp. 125-151.
- [38] Steindl, J. (1952) Maturity and stagnation in American capitalism. Oxford: Black-well.
- [39] Stockhammer, E., Onaran, Ö. and Ederer, S. (2007) "Functional income distribution and aggregate demand in the Euro-area." Department of Economics Working Papers wuwp102, Vienna University of Economics and B.A. Forthcoming in *Cambridge Journal of Economics*.
- [40] Taylor, L. (1985) "A stagnationist model of economic growth". Cambridge Journal of Economics, 9, pp. 383-403.
- [41] Tobin, J. (1986) "The Future of Keynesian Economics." Eastern Economic Journal, Vol. 12(4), pp. 347-356.